# Equivalent Near-Field Corner Frequency Analysis of 3D Dynamic Rupture Simulations Reveals Dynamic Source Effects

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## Abstract

Dynamic rupture simulations generate synthetic waveforms that account for nonlinear source and path complexity. Here, we analyze millions of spatially dense waveforms from 3D dynamic rupture simulations in a novel way to illuminate the spectral fingerprints of earthquake physics. We define a Brune-type equivalent near-field corner frequency  $(f_c)$  to analyze the spatial variability of ground-motion spectra and unravel their link to source complexity. We first investigate a simple 3D strike-slip setup, including an asperity and a barrier, and illustrate basic relations between source properties and  $f_c$  variations. Next, we analyze > 13,000,000 synthetic near-field strong-motion waveforms generated in three high-resolution dynamic rupture simulations of real earthquakes, the 2019  $M_w$  7.1 Ridgecrest mainshock, the  $M_w$  6.4 Searles Valley foreshock, and the 1992  $M_{\rm w}$  7.3 Landers earthquake. All scenarios consider 3D fault geometries, topography, off-fault plasticity, viscoelastic attenuation, and 3D velocity structure and resolve frequencies up to 1-2 Hz. Our analysis reveals pronounced and localized patterns of elevated  $f_c$ , specifically in the vertical components. We validate such  $f_c$  variability with observed near-fault spectra. Using isochrone analysis, we identify the complex dynamic mechanisms that explain rays of elevated  $f_c$  and cause unexpectedly impulsive, localized, vertical ground motions. Although the high vertical frequencies are also associated with path effects, rupture directivity, and coalescence of multiple rupture fronts, we show that they are dominantly caused by rake-rotated surface-breaking rupture fronts that decelerate due to fault heterogeneities or geometric complexity. Our findings highlight the potential of spatially dense ground-motion observations to further our understanding of earthquake physics directly from near-field data. Observed near-field  $f_c$  variability may inform on directivity, surface rupture, and slip segmentation. Physics-based models can identify "what to look for," for example, in the potentially vast amount of near-field large array or distributed acoustic sensing data.

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Supplemental Material

## Introduction

The advances of seismic array analysis (e.g., Rost and Thomas, 2002; Dougherty *et al.*, 2019; Arrowsmith *et al.*, 2022), the rise of distributed acoustic sensing (DAS, e.g., Zhan, 2019) and detailed displacement analysis using high-rate Global Navigation Satellite Systems networks (e.g., Madariaga *et al.*, 2019; Paziewski *et al.*, 2020) highlight the potential of dense ground-motion observations. Near-field recordings of well-instrumented earthquakes (Sieh *et al.*, 1993; Chung and Shin, 1999; Langbein *et al.*, 2005; Ross *et al.*, 2019) have revealed large variability of ground motions, which may originate from local site, path, and source effects (Shakal *et al.*, 2006; Ripperger *et al.*, 2008). For example, Olsen *et al.* (2008) report

"star burst patterns" of increased ground-motion peak values radiating out from the San Andreas fault where a dynamic rupture pulse changes abruptly in either speed, direction, or shape.

Concurrently, numerical forward simulations of earthquakes, combining realistic modeling of seismic sources and wave propagation, have advanced tremendously over the last decades and can provide realistic and spatially dense ground-

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motion synthetics. Earthquakes on prescribed finite-fault geometries are modeled using kinematic (Ben-Menahem, 1962; Haskell, 1964) or dynamic (Andrews, 1976; Madariaga, 1976) approaches. Kinematic models prescribe coseismic slip evolution and are computationally more efficient but do not guarantee a physically consistent source description (e.g., Tinti et al., 2005). Dynamic rupture models provide mechanically viable descriptions of how faults yield and slide based on laboratory-derived friction laws and can provide physics-based correlations among macroscopic earthquake rupture parameters, such as slip rate and rupture time (Guatteri et al., 2004; Schmedes et al., 2010; Savran and Olsen, 2020; Vyas et al., 2023). High-performance computing allows deterministic modeling of the broadband seismic wavefield in the near field of kinematic and dynamic earthquake models across the bandwidth of relevance for earthquake engineering (e.g., Heinecke et al., 2014; Withers et al., 2018; Rodgers et al., 2019; Taufiqurrahman et al., 2022). A high degree of realism of 3D physics-based forward simulations can be achieved by integrating observational data sets, such as high-resolution velocity structure and topography (e.g., Small et al., 2017; Pitarka et al., 2021), as well as physically relevant mechanisms beyond elasticity and simple source geometries, such as fault zone plasticity, viscoelastic attenuation, and fault roughness and segmentation (e.g., Shi and Day, 2013; Roten et al., 2017; Wollherr et al., 2019; Li, Gabriel, et al., 2023; Taufiqurrahman et al., 2023).

Various connections between earthquake source complexity and the variability of observed and modeled strong ground motions have been identified. Surface breaking of dynamic rupture can cause large fault-parallel ground velocity pulses (Kaneko and Goto, 2022). High-frequency and high-intensity radiation that dominates ground acceleration can be generated by abrupt changes in rupture velocity, heterogeneity of slip or slip rate, or variations in fault geometry (Madariaga, 1977, 1983; Spudich and Cranswick, 1984; Hartzell et al., 1996; Madariaga et al., 2006; Shi and Day, 2013). Small-scale ruptures in laboratory experiments and large earthquakes analyzed using backprojection emit high-frequency radiation close to the rupture tip (e.g., Marty et al., 2019; Li et al., 2022). Pulido and Dalguer (2009) analyzed the high-frequency radiation of large stress-drop regions ("asperities") and areas with a larger strength excess than their surroundings ("barriers"). They found that most of the high-frequency radiation during the 2000 Tottori earthquake originated from only 20% of the total asperity area, thereby highlighting the local character of the generating mechanism(s). Envelope inversions of ground accelerations show that high-frequency waves radiate mainly near the periphery of the fault plane or at the boundary of large slip areas (Zeng et al., 1993; Kakehi and Irikura, 1996). Using a hybrid backprojection method, Okuwaki et al. (2014) observed that strong high-frequency radiation precedes the large asperity rupture of the 2010  $M_{\rm w}$  8.8 Chile earthquake.

Recent observational data analyses imply that high-frequency radiation may strongly correlate with fault trace "misalignment" (Chu et al., 2021), that is, geometric fault complexity. Adda-Bedia and Madariaga (2008) showed theoretically that a rupture front turning at a fault kink generates a burst of high-frequency radiation aligned with a jump in particle velocity, which has also been observed in 3D dynamic and kinematic rupture simulations (Oglesby and Mai, 2012; Li et al., 2022). Zhang and Ge (2017) reported peaks in highand low-frequency seismic energy release at a stepover rupture during the 2014  $M_{\rm w}$  7.0 Yutian earthquake. Dynamic rupture models of stepover faults (e.g., Lozos et al., 2014) show highfrequency peak ground velocity bursts radiating beyond the slipping faults (Hu et al., 2018). While rupture directivity affects dominantly low- and intermediate-frequency bands, it can cause most of the seismic energy from a finite rupture to arrive as a single large pulse and may increase the components' average high-frequency radiation in a magnitudedependent frequency band (Somerville et al., 1997; Kane et al., 2013). The strength of directivity effects depends on the ratio of the mean rupture velocity to wave propagation velocity (Boore and Joyner, 1978). 3D dynamic rupture simulations have shown that off-fault plasticity causes near-fault peak ground velocities to saturate and increases the dominant period of such a directivity pulse (Wang and Day, 2020).

However, identifying and physically interpreting observable near-field ground-motion complexities remains challenging. Theoretical source models often assume simple, for example, circular, source geometries, and a constant subshear/sub-Rayleigh rupture speed. Dynamic rupture simulations have demonstrated that this is rarely the case for large earthquakes (e.g., Ulrich, Gabriel, et al., 2019; Ulrich, Vater, et al., 2019; Harris et al., 2021; Yu et al., 2022; Jia et al., 2023). Recent observational studies show that also small events exhibit considerable rupture complexity and that their spectra often deviate from simple circular ( $\omega^2$  decay) source models (e.g., Fan and McGuire, 2018; Pennington et al., 2023; Yoshida and Kanamori, 2023). But even for the best-recorded earthquakes, observations often miss the spatial resolution required to uniquely relate ground-motion variability to source complexity.

Here, we aim to systematically relate the spectral properties of synthetic strong ground motions from 3D dynamic rupture earthquake scenarios to physics-based source complexity. We analyze millions of synthetic waveforms from dynamic rupture simulations to illuminate the spectral fingerprints of earthquake source mechanisms in the near field. We define a spatially variable Brune-type (Brune, 1970) corner frequency  $f_c$  as a scalar proxy of a waveform's relative frequency content to analyze its variability in the vicinity of rupturing fault systems and associate it with different aspects of source complexity. We term  $f_c$  as the equivalent near-field corner frequency to avoid any confusion with far-field corner frequency analysis. We analyze four 3D dynamic rupture models of increasing complexity for which we generate spatially high-resolution groundmotion synthetic seismograms. We identify distinct spatial patterns in  $f_c$  that are associated with fault geometry complexity, rupture directivity, surface rupture, or variable slip distribution. We use isochrone theory (Bernard and Madariaga, 1984; Spudich and Cranswick, 1984) to locate the sources of high-frequency radiation and to interpret our results.

## Methods

## Equivalent near-field corner frequency

The average corner frequency of far-field source spectra can be used to estimate an event's stress drop (e.g., Brune, 1970; Thatcher and Hanks, 1973; Allmann and Shearer, 2009; Abercrombie, 2021), which requires a theoretical model of the source. The classical Brune (1970) model describes the displacement amplitude spectrum A(f) of far-field body waves as follows:

$$A(f) = \frac{\Omega_0}{1 + (f/f_c)^2},$$
(1)

in which  $\Omega_0$  is the amplitude of the lowest frequency of the spectrum;  $f_c$  is the corner frequency; and f is a well-defined frequency band. The Brune-type spectrum is flat at low frequencies, with  $\Omega_0$  proportional to the seismic moment  $M_0$ , and it has an  $\omega^{-2}$  fall-off rate at high frequencies. The corner frequency  $f_c$  marks the transition between the two parts of the spectrum.

In this study, we aim to analyze the relative spatial variability of simulated spectra in the near field in distinction to inferring source properties, such as source dimensions or stress drop. Although we model not exclusively the near field, we focus on near-field effects (see Appendix). In all our models, the respective S-wave travel times from the slipping faults to the model domain boundaries correspond to 2-3 times the respective rupture duration. We adapt the classical Brune (1970) model (equation 1) to determine near-field spectral corner frequencies. We acknowledge that our application violates some of Brune (1970) underlying theoretical assumptions: our simulated waveforms include nonnegligible near-field terms, the effects of topography and 3D velocity structure, and a clear separation between P- and S-wave spectra is mostly impossible because the event durations are longer than the arrival-time differences (e.g., Madariaga et al., 2019). Thus, we term the inferred spectral waveform property the equivalent near-field corner frequency  $(f_c)$ .

First, we rotate the horizontal components of all synthetic seismograms into radial and transverse components with respect to the absolute slip centroid of the respective dynamic rupture model. We then apply a tapered body-wave window to each time series to mitigate the impact of later arriving surface waves. The body-wave window effect is generally small, except in the Searles Valley dynamic rupture simulation. The bodywave window starts at the *P*-wave arrival time. Its length is chosen as the rupture duration of the respective dynamic rupture scenario added to an *S*-wave delay specifically calculated for each virtual station based on its distance to the slip centroid. Notably, using this body-wave window prevents a deflected high  $f_c$  ray in the Searles Valley foreshock dynamic rupture scenario from affecting our analysis. In other scenarios, its effect is negligible. With this approach, we disregard time-dependent frequency content and focus our analysis on spatial variability.

Next, we Fourier transform the velocity waveforms and integrate the spectra by division with  $i\omega$ . The order of these operations is important because computing the Fourier transform of an already integrated displacement time series, which potentially contains static displacement and is thus not periodic, can lead to spectra that are contaminated at all frequencies (Madariaga *et al.*, 2019). In the next step, we resample the spectrum to equally spaced sampling points up to the numerically resolved maximum frequency of each simulation (see Appendix). An alternative approach would be to resample the spectrum to a logarithmic spacing (e.g., Ide *et al.*, 2003).

We solve equation (1) for all possible  $f_c$  values in 0.005 Hz steps between the inverse of the body-wave window (always <0.1 Hz) and 1.0 Hz and evaluate the misfits between the simulated and analytical spectra. We define the equivalent nearfield corner frequency as the value of all possible  $f_c$  values, which leads to the smallest misfit. Theoretically,  $\Omega_0$  in equation (1) is given by the amplitude of the lowest frequency of the respective spectrum. However, the fit can be generally improved by considering a mean amplitude value of the lowfrequency part (e.g., Trugman, 2020). Here, we choose the mean value of the lowest frequency up to the respective  $f_c$ , which renders our approach robust for spectra that contain static displacements and are not flat at the low-frequency part (e.g., station CLC in Fig. S5, available in the supplemental material to this article). This approach differs from the classical Brune model in which the amplitude is half of the long-period level at  $f_c$ . However, this does not lead to a systematic underestimation at long-period levels (Figs. S5 and S6).

We use the spectral seismological misfit approach of Karimzadeh *et al.* (2018) for corner frequency picking:

$$\text{Misfit}_{\text{SS}} = \frac{1}{n_f} \sum_{i=1}^{n} \left| \log \frac{A(f_i)}{A_{\text{Brune}}(f_i)} \right|,\tag{2}$$

in which  $f_i$  are the discrete sample points of the spectra; and  $n_f$  is the absolute number of sample points.  $A(f_i)$  are the spectral amplitudes of the synthetic waveforms and  $A_{\text{Brune}}(f_i)$  are the amplitudes of the respective Brune-type spectra (equation 1). This approach has two major benefits compared with a root mean square misfit. It is based on relative differences and, therefore, is independent of the examined absolute amplitudes.

In addition, its logarithmic scaling prevents overweighting of outliers in strongly oscillating spectra (e.g., Lindley and Archuleta, 1992).

We compute  $f_c$  using parallelized Python code and exploiting efficient NumPy tensor operations (Harris *et al.*, 2020). We openly provide our code (see Data and Resources) that automatically facilitates the loading of raw waveform data, preprocessing, and calculation of  $f_c$ . For example, our script requires ~23 min to process 3,000,000 waveforms of the Landers earthquake dynamic rupture scenario using 30 processes. Input data loading is also parallelized but does not optimally scale and uses ~50% of the computational runtime. We perform the computations on an AMD EPYC 7662 64-Core processor with a 2 GHz clock speed.

## **Isochrone theory**

We use isochrone theory (Bernard and Madariaga, 1984; Spudich and Frazer, 1984) to interpret the equivalent near-field corner frequency distributions. Isochrone theory assumes that close to large earthquakes, most high-frequency ground motions are caused by direct *P* and *S* waves generated at the rupture front (Madariaga, 1983; Spudich and Cranswick, 1984; Marty *et al.*, 2019). Under this assumption, high-frequency ground motions recorded at a station can be derived from a series of line integrals instead of using the full surface integral of the representation theorem.

In the framework of isochrone theory, the integration path for each time step consists only of points on the fault associated with the high-frequency radiation that arrives at the observer at the respective time step. These lines are called isochrones and are contour lines of the sum of the rupture times and travel times to the respective station. Rupture time is defined as the time at which the absolute slip rate at a point on the fault exceeds 0.001 m/s. The ground velocities can be directly related to the isochrone velocity c, which is proportional to the isochrone spacing as follows:

$$c(x,z,\underline{r}) = |\nabla_s t(x,z,\underline{r})|^{-1}, \qquad (3)$$

and  $\nabla_s$  is the surface gradient with respect to the fault coordinates (x,z); t is the isochrone time (the sum of the rupture time and travel time); and  $\underline{r}$  are the coordinates of the station. Points on the fault in which c is singular radiate particularly high frequencies. A prominent example is supershear rupture and its associated *S*-wave Mach cones (Spudich and Frazer, 1984). Spatial variations in the slip velocity and temporal variations in the isochrone velocity can cause comparable ground accelerations. Seismic directivity decreases isochrone spacing, thereby increasing isochrone velocity (Spudich and Chiou, 2008). Thus, isochrone analysis inherently captures the contributions of near-field directivity effects.

To use isochrone theory to analyze complex dynamic rupture scenarios, here, we mostly use the peak slip-rate time instead of the rupture (initiation) time. Peak slip-rate time is also associated with the rupture front but is often smoother and less prone to ambiguity, for example, due to multiple rupture (and healing) fronts. We only assign peak slip-rate times to points on the fault where the peak slip rate exceeds 0.05 m/s for TPV5 and 0.1 m/s for the Ridgecrest and Landers dynamic rupture models. In the following, we mostly show peak sliprate times inferred from the dip-slip components to separate the vertical slip from the strike-parallel slip and to isolate the effects of rake-rotated rupture fronts.

## Results

We analyze the waveforms generated in 3D dynamic rupture simulations of a simple community benchmark setup and three large-scale scenarios of real earthquakes. All four dynamic rupture scenarios are detailed in the Appendix. In the following, "high-frequency" refers to frequencies higher than approximately twice the inverse of the event duration, which is 0.22 Hz for the community benchmark TPV5, 0.2 Hz for the Searles Valley foreshock, 0.14 Hz for the Ridgecrest mainshock, and 0.11 Hz for the Landers earthquake dynamic rupture scenarios. For the latter, we exclude the last and smallest subevent on the Camp Rock fault in this approximation, which increases rupture duration but contributes weakly to the seismic moment.

#### TPV5 3D dynamic rupture community benchmark

We demonstrate the relationship between the source properties, high-frequency radiation, and equivalent near-field corner frequency variations using the TPV5 U.S. Geological Survey / Southern California Earthquake Center (USGS/SCEC) 3D dynamic rupture community benchmark (Harris *et al.*, 2009). The benchmark's domain is a homogeneous elastic half-space; therefore, no path or site effects affect our analysis. We model a bilateral strike-slip dynamic rupture passing an asperity and a barrier, regions with elevated or reduced initial shear stresses, which significantly accelerate or decelerate the rupture, respectively (Fig. 1d).

Figure 1e-h shows two pairs of isochrone contours on the fault plane and acceleration waveforms of the respective virtual stations. Isochrones in Figure 1e are calculated by adding the S-wave travel time at station T1 (located at x = -10 km and y = 30 km; Fig. 1b) to the rupture time. The patch in the middle represents the overstressed nucleation area. The rupture acceleration due to the left asperity causes an increased isochrone spacing to the left side of the hypocenter and vice versa the rupture deceleration due to the right barrier causes a decrease in isochrone spacing to the right side of the hypocenter. Figure 1f shows the corresponding acceleration time series of the transverse component at T1. Ground accelerations are generally associated with high-frequency radiation and are proportional to changes in the isochrone spacing (Spudich and Frazer, 1984). Every pronounced high-amplitude signal in the accelerogram can be related to a specific rupture



**Figure 1.** TPV5's equivalent near-field corner frequency ( $f_c$ ) distribution of the (a) radial, (b) transverse, and (c) vertical components of synthetic seismograms recorded at ~900,000 virtual seismic stations in map view. The seismograms are generated in a bilateral strike-slip 3D dynamic rupture model including an asperity and a barrier embedded in a homogeneous elastic half-space (the TPV5 Southern California Earthquake Center [SCEC]/U.S. Geological Survey [USGS] community benchmark, Harris *et al.*, 2009). The black lines indicate the fault trace, the star marks the hypocenter, and white triangles are stations that are analyzed in panels (e–h). The orange lines mark different high- $f_c$  features. (d) Side-view of the fault plane with rupture front contours in 0.5 s intervals. (e) Isochrone contours of station T1 in 0.5 s intervals. (f) Transverse ground accelerations at station T1. Comparison with isochrones allows associating pronounced high-amplitude signals with different stages of 3D dynamic rupture propagation. Acc., acceleration; dec., deceleration; asp., asperity. (g) Peak dip-slip isochrone contours of station T2 in 0.5 s intervals. (h) Vertical ground accelerations at station T2. The color version of this figure is available only in the electronic edition.

phase by comparing the time step with the respective isochrone. For example, the accelerogram oscillations at 10 s are caused by the nucleation, the two spikes at 11.5 and 12.5 s represent the acceleration and deceleration at the high-stress asperity, and the strongest pulse at 14.5 s results from stopping phases when rupture reaches the prescribed left end of the fault.

Figure 1g shows the peak dip-slip isochrones (the sum of the S-wave travel time and peak dip-slip time) at station T2 (located at x = -35 km and y = 25 km; Fig. 1c). Those points on the fault with peak dip-slip rates of less than 0.05 m/s are ignored because their contribution to the radiated waves is negligible. We use a median filter favoring the dominant isochrones to avoid oscillations in which different rupture fronts have a comparable peak slip rate. Figure 1h shows the vertical ground accelerations at station T2, which are dominated by a single spike shortly after 16 s. Isochrone analysis reveals that this spike is caused by a phase of dip-slip acceleration and abrupt rupture arrest induced by a surface-reflected rupture front. The large isochrone spacing (after 16 s, Fig. 1g) at the upper left side of the fault shows this strongly accelerating dip-slip phase that abruptly stops at the left fault end. The dip-slip phase originates from rake rotation at the dynamic rupture front, which is larger at shallow depths and is significantly amplified when the rupture breaks the surface (Oglesby et al., 2000). Such shallow rake rotation has been linked to geological features

(a) TPV5: rake at t = 6 s

(b) Ridgecrest mainshock: average rake





(C) Landers: average rake



such as slickenlines (Kearse and Kaneko, 2020) and increased tsunami hazards of strike-slip fault systems (Kutschera *et al.*, 2023; Li, Gabriel, *et al.*, 2023).

Important, the equivalent near-field corner frequency  $f_c$ is not a direct measure of the high-frequency content of the modeled seismic wavefield but rather reflects a relative association between high and low frequencies. Figure 1a–c shows the  $f_c$  distribution of the radial, transverse, and vertical components of the synthetic seismograms recorded at ~900,000 virtual stations in map view. We observe pronounced variability in  $f_c$ . A thin ray of high  $f_c$  in fault-normal direction, visible in the radial and vertical components (Fig. 1a,c), reflects the nodal line of the *P*–*SV* radiation pattern and is also present in other corner frequency studies of (near) symmetrical ruptures (e.g., Kaneko and Shearer, 2015; Wang and Day, 2017) and in spectral estimates using data of the Large-*n* seismic survey in Oklahoma (LASSO; Kemna *et al.*, 2020).

Rays of high  $f_c$  form in the transverse components (Fig. 1b) at an angle of ~45° to the rupture propagation direction. These reflect the nodal planes of a strike-slip *SH* radiation pattern centered at the hypocenter. The radiation pattern affects low frequencies stronger than high frequencies (e.g., Takemura *et al.*, 2009; Trugman *et al.*, 2021), which leads to a lack of low-frequency energy at the nodal planes and thus locally increases the measured  $f_c$ .

**Figure 2.** (a) Rake at t = 6 s of the TPV5 dynamic rupture model (Harris *et al.*, 2009). (b) Average rake of the 2019  $M_w$  7.1 Ridgecrest mainshock dynamic rupture model (Taufiqurrahman *et al.*, 2023). (c) Average rake of the 1992  $M_w$  7.3 Landers dynamic rupture model (Wollherr *et al.*, 2019). The color version of this figure is available only in the electronic edition.

We observe two raylike high- $f_c$  patterns at approximately the same 45° angle to the fault trace in the vertical components (Fig. 1c), for example, where station T2 is placed. We link these to the high-amplitude lobes of a strike-slip P-SV radiation pattern in the rupture-forward direction of a vertical high-frequency pulse caused by a rapidly accelerating and decelerating phase of dip-slip during surface-breaking rupture, as shown in the isochrones in Figure 1g. We quantify the rake rotation related to shallow dip-slip to be only up to 10° (Fig. 2a). Thus, the overall radiation is dominated by the strike-slip radiation pattern. Directivity effects additionally sharpen the vertical ground-motion pulse and contribute to the high  $f_c$ . The vertical-component high- $f_c$  bands are of considerably lower amplitudes on the right side of the model domain. This is caused by the differences in bending of the rupture front due to either high- or low-shear stress patches (Fig. 1d). Convex bending due to the submerged left, high-shear stress asperity leads to more abrupt decelerating of the surface-reflected rupture front, generating more high-frequency radiation.

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#### 2019 Ridgecrest sequence

We analyze the relationship between the equivalent near-field corner frequency  $f_c$ , isochrones, and source complexity in Taufiqurrahman et al. (2023) 3D dynamic rupture scenario for the 2019  $M_{\rm w}$  7.1 Ridgecrest mainshock. We also analyze the  $f_c$  distribution of their Searles Valley foreshock dynamic rupture model, which reveals additional path effects. In the following, we refer to the dominant impact of the 3D velocity structure as "path effects" and not to the effects of the also modeled intrinsic viscoelastic attenuation, which may become more relevant at higher frequencies than considered here. We do not include (nonlinear) site effects in our models (Hu et al., 2021; Roten et al., 2023) as the surface S-wave velocities considered in our models are mostly higher than 1.5 km/s (with exceptions being the Salton Sea basin and the San Bernardino basin in the Landers model), and elastic moduli do not change due to the passage of seismic waves (e.g., Niu et al., 2023). Figure 3 provides an overview of both dynamic rupture models, and the Appendix includes a detailed description.

The Ridgecrest mainshock dynamic rupture scenario ruptures primarily along a northwest-southeast-trending continuous fault (F3 in Fig. 3c). The rupture starts as a bilateral crack that expands away from the hypocenter. After 5 s rupture time, it terminates to the north due to a locally lower prestress and a less optimal fault orientation. The southward rupture cannot break through the conjugate F2–F3 intersection at shallow depths due to the stress shadow caused by the foreshock dynamic rupture scenario (Taufiqurrahman *et al.*, 2023). Only deep decelerated slip "tunnels" the intersection and regrows as a pulse that ruptures again to the surface and to the southeastern end of F3.

Figure 4 shows the  $f_c$  distribution of the three components of the Ridgecrest mainshock dynamic rupture simulation, complemented by a map of the regional topography incorporated into the model and the fault system surface traces. For each component, the equivalent near-field corner frequencies are computed at ~1,800,000 virtual seismic stations with a spacing of ~500 m. The vertical components exhibit particularly high spatial variability in the inferred  $f_c$ .

We find that the directivity effects associated with the bilateral rupture lead to an elevated  $f_c$  at both ends of the main fault in the radial and vertical components (Fig. 4a,c and red dashed lines in Fig. 5d). The corner frequency variability of the transverse component (Fig. 4b) is smaller than that of the other components and resembles to first-order a strike-slip radiation pattern:  $f_c$  is higher close to the nodal planes and lower where the wavefield amplitudes are expected to be the largest.

A gap between two high- $f_c$  rays in the vertical components (orange lines in Fig. 5d) is related to a major rupture complexity of the mainshock, the "tunneling" dynamics at the intersection with the orthogonal fault F2 (Fig. 3c). We compare the modeled acceleration waveforms at synthetic stations located

within the elevated- $f_c$  regions (stations R1 and R3) with a station located in the gap between the high- $f_c$  rays (station R2) in Figure 5a–c. The waveforms show that regions with high- $f_c$  values are associated with a high-frequency acceleration pulse that is absent in the R2 accelerogram.

Figure 5e,f shows the corresponding peak dip-slip isochrones at high- $f_c$  stations R1 and R3, which we use to identify the origin of the acceleration pulses. The acceleration pulse at R1 occurs shortly after 17 s simulation time. This 17 s pulse originates from an "isochrone jump" at the intersection with the orthogonal fault F2 close to the surface. This isochrone jump is caused by the abrupt stopping of the rupture at the intersection at shallow depth and delayed activation of the fault area behind the intersection. The complex shape of the peak dip-slip isochrones in the shallow area before the fault intersection (Fig. 5e) is caused by a secondary surface-reflected rupture front, which involves a pronounced rake rotation (Fig. 2b). The complex dynamics of surface rupture, rake rotation, and abrupt rupture arrest at the geometric barrier formed by the fault intersection conjointly generate pronounced high-frequency radiation in the vertical component. The high- $f_c$ ray, in which R1 is located (Fig. 5d), reflects a high-amplitude lobe in the rupture-forward direction of a P-SV radiation pattern of this high-frequency dynamics.

The same mechanism of surface dynamic rupture, rake rotation, and arrest explains the high acceleration pulse recorded at R3. This pulse occurs at 20 s, which coincides with the surface-breaking and rake-rotated rupture front stopping abruptly at the southern end of the fault system. Its amplitude is higher because this station is closer to the fault, the directivity effect is stronger, and rupture deceleration may appear as more abrupt. The isochrones show the first upgoing rupture front, whereas the vertical acceleration pulses are associated with the deceleration of the surface-reflected rupture front. This leads to a timing discrepancy of  $\sim$ 1 s between the high-frequency pulse in the accelerogram and the rupture stopping indicated by the isochrones.

The spectra of the observed near-field vertical ground motions show similar spatial variability in  $f_c$  as the dynamic rupture model of the 2019 Ridgecrest mainshock. In Figure 5d, we show the vertical  $f_c$  values of the observed spectra at 17 near-field stations (Fig. S5). The observed  $f_c$  values depend on azimuth and mostly resemble the synthetic  $f_c$ map. Six stations are located in rupture forward direction at the northern end of the fault system, and  $f_c$  values at four of these stations agree with our modeled values, whereas  $f_c$ at two stations is lower than in our model. We may speculate that a slightly different location of rupture arrest to the north or unmodeled site effects cause this discrepancy. The station with the highest observed  $f_c$  is located at the southern end of the fault system where the strongest directivity is expected, which agrees with our model. Figure S5 shows that the synthetic spectra generally reproduce the observed spectra. The



**Figure 3.** Overview of the 2019 Ridgecrest sequence (linked  $M_{\rm w}$  6.4 Searles Valley foreshock and  $M_{\rm w}$  7.1 Ridgecrest mainshock) 3D dynamic rupture models adapted from Taufiqurrahman *et al.* (2023). (a) Fault geometry with slip distribution after both earthquakes and crosscut of the unstructured tetrahedral computational mesh colored by the used 3D variable *S*-wave velocity (CVM-S4.26; Lee *et al.*, 2014). (b) Seismic

moment release rate for both foreshock and mainshock. (c) Slip rate snapshots across the orthogonal fault system at selected rupture times, illustrating dynamic rupture evolution and complexity. The foreshock dynamic rupture scenario is shown on the left side, and the mainshock is on the right side. The color version of this figure is available only in the electronic edition.



observed spectra fit the Brune model to first order; however, local deviations in limited frequency bands also occur.

The dynamic rupture model of the Searles Valley foreshock initiates close to the F1–F2 fault intersection (Fig. 3c). Rightlateral slip on F1 spontaneously ceases without reaching the surface, which agrees with observations (Liu *et al.*, 2019). The deep rupture on F1 activates the conjugate, critically prestressed left-lateral fault F2. F2 ruptures entirely to its southwestern end, accumulating most of the event's slip and breaking the surface over its full length.

Although both events, the mainshock, and the foreshock, are rupturing the same fault system, their vertical  $f_c$  distributions differ vastly. This illustrates that  $f_c$  is dominated by source effects. In Figure 6d we observe a wide  $f_c$ -shadow zone, an area of smaller than average  $f_c$ , in the rupture backward-directivity direction (northeast), which reflects the dominantly unilateral nature of the foreshock rupture. A thin ray of elevated  $f_c$  within this shadow zone emits from the small

**Figure 4.** Map view of the Ridgecrest mainshock's equivalent near-field corner frequency ( $f_c$ ) distribution of the (a) radial, (b) transverse, and (c) vertical components of synthetic seismograms simulated at ~1,800,000 virtual seismic stations. The synthetic seismograms are generated from the complex 3D dynamic rupture model of the 2019 Ridgecrest mainshock (Fig. 3). (d) Map view of the model's topography. The black lines indicate the numbered fault traces, triangles show near-field station locations, and the star marks the epicenter. The color version of this figure is available only in the electronic edition.

nonsurface rupturing slip patch at the northwest-trending F1 (Fig. 3c). Our results show high- $f_c$  structures (highlighted with dashed orange lines in Fig. 6d) pointing away from the southwestern part of the primary fault F2, where the rupture breaks the surface. A gap in these high- $f_c$  rays coincides with a small kink of the fault trace.

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A pronounced feature in the vertical  $f_c$  distribution of the Searles Valley foreshock is a curved-path high- $f_c$  ray (dashed red line in Fig. 6d), which changes direction from west-northwest to northeast. Its bent structure is caused by deflection at the strong velocity contrast along the southern Sierra Nevada mountain range (Fig. 4d). An animation of the 3D wavefield (see Data and Resources) illustrates these locally strong path effects.

Seismic energy is directed in unexpected directions and significantly prolongs the observed shaking duration at several stations, for example, at station WMF. Figure 6a-c shows synthetic and observed waveforms at station WMF, which are low-pass filtered at 0.5 Hz. In this frequency range, the synthetic ground motions of the directly arriving wave packet agree well with the observations (before 40 s). For the second wave packet, which is associated with the deflection at the **Figure 5.** (a,b,c) Ridgecrest mainshock's synthetic vertical ground accelerations at three selected stations. (d) Map view of the equivalent near-field corner frequency ( $f_c$ ) distribution of the vertical components of synthetic seismograms recorded at ~1,800,000 virtual seismic stations. The synthetic seismograms are generated from a complex dynamic rupture model of the 2019 Ridgecrest mainshock (Fig. 3). The black lines indicate the fault traces, the star marks the epicenter, colored dots show  $f_c$  values of recorded ground motion spectra, and triangles show the virtual station locations of the analyzed accelerograms. The orange and red lines mark different high- $f_c$  features. (e,f) Peak dip-slip isochrones of stations R1 and R3. The color version of this figure is available only in the electronic edition.

mountain range, there are significant differences between the synthetic and observed waveforms. The synthetic wave packet arrives earlier, has a shorter duration, and contains



single high-frequent spikes in the EW and Z components. These differences may be explained by a lack of small-scale subsurface heterogeneity in the 3D velocity model used in the dynamic rupture simulation. Additional high-frequency wave scattering may prolong coda-shaking (e.g., Imperatori and Mai, 2012; Takemura et al., 2015; Taufiqurrahman et al., 2022). The travel-time difference may be caused by underestimating the velocity reduction of a sedimentary basin between the mountain range and the fault system in the used 3D velocity model (CVM-S4.26; Lee et al., 2014). To not omit late-arriving deflected waves, we derive  $f_c$  values in Figure 6d from the full-time series of the simulation (100 s duration after the nucleation) without picking a body-wave window. The same plot with selecting a body-wave window is shown in Figure S2. The body-wave window removes the curved high- $f_c$  ray, but otherwise, the  $f_c$  distribution is nearly identical.

## 1992 Landers earthquake

The dynamic rupture model of the 1992 Landers earthquake by Wollherr *et al.* (2019) ruptures across five fault segments (Fig. 7, and for an animation see Data and Resources). Rupture nucleates at the southern part of the Johnson Valley fault (JVF) and propagates northward. After 4 s, the rupture migrates to the Kickapoo fault (KF) by direct branching. The Kickapoo fault connects the rupture from the JVF to the Homestead Valley fault (HVF). The rupture nearly stops at a fault bend at the HVF but then reinitiates **Figure 6.** Searles Valley foreshock's synthetic and observed velocity seismograms of the (a) east (E), (b) north (N), and (c) up (Z) components at station WMF. In difference to Taufiqurrahman *et al.* (2023), we here show seismograms not normalized and including higher frequencies, low-pass filtered to 0.5 Hz to highlight the match of the first wave packet. (d) Map view of the equivalent near-field corner frequency ( $f_c$ ) distribution of the vertical components of synthetic seismograms simulated at ~1,800,000 virtual seismic stations (without picking a body-wave window). The seismograms are generated from the complex 3D dynamic rupture model of the 2019 Searles Valley foreshock (Fig. 3). The black lines indicate the fault traces, the star marks the epicenter, and the triangle shows the location of the station WMF. The color version of this figure is available only in the electronic edition.

and breaks up to its northern extent. Although rupturing the HVF, a second rupture front branches to the Emmerson fault (EF). At around 15.5 s, a part of the EF is also activated by dynamic triggering from waves generated at the northern part of the HVF. Multiple rupture fronts (including backpropagating rupture fronts) form when the slower rupture front from direct branching reaches the part of the EF that was dynamically triggered. The backward propagating rupture dynamically reactivates parts of the HVF and the KF. After 22.3 s, a completely separate subevent on the Camp Rock fault (CRF) is dynamically triggered by the superimposed waves generated at the EF and the northern part of the HVF. The rupture completely stops after 30 s.

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**Figure 7.** Overview of the 1992 Landers earthquake 3D dynamic rupture model adapted from Wollherr *et al.* (2019). (a) Fault geometry with accumulated slip distribution and crosscut through the unstructured tetrahedral computational mesh colored by the used 3D variable *S*-wave velocity (Shaw *et al.*, 2015). (b) Seismic moment release rate. The Landers dynamic rupture model (preferred model, orange) is compared to the optimal and average moment rate release of the SCARDEC database (in black and dotted light gray, Vallée and Douet, 2016) and the inferred

moment rate based on the surface slip (in light blue, Kagan and Houston, 2005). CRF, Camp Rock fault; EF, Emerson fault; HVF, Homestead Valley fault; KF, Kickapoo fault; JVF, Johnson Valley fault. (c) Slip rate snapshots across the fault system at selected rupture times illustrating dynamic rupture evolution and complexity. Rupture cascades across fault segments through direct branching and dynamic triggering. The color version of this figure is available only in the electronic edition.



Figure 8a-c shows the equivalent near-field corner frequency  $f_c$  distributions of the Landers dynamic rupture simulation computed at ~1,000,000 virtual seismic stations. The vertical components, as well as parts of the radial components, exhibit considerable spatial variability in the inferred  $f_c$ , whereas the spatial variability of  $f_c$  of the transverse components is lower. The vertical component shows a complex pattern of localized rays of increased  $f_c$ , pointing away from the fault trace. We observe a correlation between the distribution of  $f_c$  in the vertical and radial components, which we interpret as an indication that the *P*-SV wave modes are responsible for the observed rays.

Sharp changes of  $f_c$  outline several low-velocity sedimentary basins, such as the Salton Sea basin in the South and the San Bernardino and Los Angeles basins in the southwest. Lowvelocity sediment basins lead to sharp corner frequency increases of the *P*–*SV* mode at their edges. Although this is a plausible mechanism, we here clip the color map at **Figure 8.** Map view of the Landers earthquake's equivalent nearfield corner frequency ( $f_c$ ) distribution of the (a) radial, (b) transverse, and (c) vertical components of synthetic seismograms simulated at ~1,000,000 virtual seismic stations. The seismograms are generated from the complex 3D dynamic rupture model of the 1992 Landers earthquake (Fig. 7). We clip the color map at sedimentary basins and close to the fault, where static displacement and an inaccurate component separation due to finite-fault effects distort the corner frequency determination. We omit these regions in our interpretation. (d) Map view of the model's topography. The black lines indicate the fault traces, triangles show station locations, and the star marks the epicenter (CRF, Camp Rock fault; EF, Emmerson fault; HVF, Homestead Valley fault; JVF, Johnson Valley fault; KF, Kickapoo fault). The color version of this figure is available only in the electronic edition.

sedimentary basins and close to the fault, where static displacement and an inaccurate component separation due to finitefault effects distort the corner frequency determination, and we omit these regions in our interpretation.



We highlight the rays of high  $f_c$  in the vertical components of the Landers model as dashed lines in Figure 9d. These rays mostly takeoff at an angle close to 45° to the rupture forward direction, and they trace the curvature of the segmented fault system. South of the epicenter,  $f_c$  is generally lower, although this is overprinted by a local increase due to the Salton Sea basin. Decreased southern  $f_c$  is caused by the directivity effects of the north-northwestward-directed unilateral rupture, which prolongs shaking in the backward direction and mitigates the high-frequency content. We note that analyzing the vertical components of the Landers model can lead to a higher average  $f_c$  because it consists of more sharply separated subevents and dip-slip patches (Fig. 7; Das and Aki, 1977).

Three seismic stations (Fort Irwin, Barstow, and Yermo), which recorded near-field waveforms of the 1992 Landers event, are located on or between our modeled rays of elevated corner frequencies. Comparing the observed spectra with our synthetic data reveals an excellent fit between 0.1 and 1.0 Hz (Fig. 9a–c). Station Fort Irwin is located between two high- $f_c$  rays and has a lower  $f_c$  than the spectra of the stations Barstow and Yermo, which are located on high- $f_c$  rays. Spectra recorded at other near-field stations agree well with the synthetic spectra between 0.1 and 1.0 Hz (Fig. S6).

We use isochrone theory to identify the source of the elevated  $f_c$  rays in the vertical components. The rupture process of the Landers model is complicated and often involves multiple rupture fronts and reactivation of slip, whereas the isochrones can capture only a single phase of slip (see the animation of the rupture process, Data and Resources).

**Figure 9.** Observed spectra and corresponding  $f_c$  of the 1992 Landers earthquake compared with synthetic counterparts at three selected stations: (a) Fort Irwin, (b) Barstow, and (c) Yermo. The spectra are not normalized but reflect absolute values. (d) Same as Figure 8c. The black solid lines indicate the fault traces, the star marks the epicenter, triangles are real station locations, and hexagons show two virtual stations that are analyzed in Figure 10. The dashed lines highlight rays of high  $f_c$ , and the text windows show the fault names where the rays originate (CRF, Camp Rock fault; EF, Emmerson fault; HVF, Homestead Valley fault; KF, Kickapoo fault ). We clip the color map at sedimentary basins and close to the fault, where static displacement and an inaccurate component separation due to finite-fault effects distort the corner frequency determination. We omit these regions in our interpretation. The color version of this figure is available only in the electronic edition.

Figure 10a,c,e shows the synthetic ground accelerations at three selected stations: Yermo and two virtual stations L1 and L2 (Fig. 9d). As expected from previous observational analysis (Campbell and Bozorgnia, 1994), directivity effects strongly affect waveforms recorded at Yermo, which is located in the average strike direction of the unilateral rupture. Therefore, Yermo's waveforms overall have a considerable amount of high-frequency shaking and do not exhibit a single spike that is solely responsible for the high  $f_c$ . However, we observe that a dynamically triggered subevent at the Camp Rock fault causes the highest waveform amplitudes at about 36 s (Fig. 10a,b). This subevent initiates at 8 km depth, breaks the surface, and terminates during a short period of time,

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which superimposes the overall source spectrum with a source spectrum of a lower magnitude subevent corresponding to a higher  $f_c$ . The same subevent causes a strong signal at about 40 s at L1.

The accelerogram at virtual station L1 is dominated by a pulse starting at about 29 s. The isochrones show that the source of the high-frequency radiation recorded at L1 is located

**Figure 10.** (a,c,e) Landers earthquake's synthetic vertical accelerograms at three selected stations: Yermo, L1, and L2 (Fig. 9d). (b,d,f) Peak dip-slip isochrones of the respective stations. The star marks the hypocenter (CRF, Camp Rock fault; EF, Emmerson fault; HVF, Homestead Valley fault; JVF, Johnson Valley fault; KF, Kickapoo fault). The color version of this figure is available only in the electronic edition.

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either at the top or at the bottom of the rupture zone of the EF. The animation of the rupture shows that a dynamically activated backpropagating rupture front coalescences with a forward-propagating rupture front, which causes high-amplitude up-dip and down-dip propagating rupture fronts (Fig. S3c,d). The down-dip propagating front arrests when it reaches the bottom of the seismogenic zone, and the up-dip propagating front breaks the surface until it stops abruptly at the kink to the CRF. This shallow surface-breaking rupture is dominant in generating the vertical acceleration pulse at L1 because it involves an average rake rotation of up to 10° (Fig. 2c), which is not observed at the bottom of the rupture zone.

The accelerogram of the virtual station L2 contains two strong high-frequency pulses, the first starting at about 16 s and the second starting at 19 s. The isochrones show that the first high-frequency pulse coincides with the surface rupture at the kink between the JVF and the KF; therefore, the source might be a so-called kink wave (Adda-Bedia and Madariaga, 2008) from the rake-rotated rupture front propagating along the surface. However, another rupture front propagates up-dip along the kink simultaneously (Fig. S3a). This coalescence of differently directed rupture fronts likely also contributes to the modeled high-frequency radiation. A similar mechanism, a coalescence of an up-dip propagating rupture front and an along-strike propagating rupture front at the fault kink between the KF and the HVF segments generates the second high-frequency pulse (Fig. S3b). There is a small discrepancy between the isochrone timing and the high-amplitude spike in the waveforms because the isochrones capture the rupture front that propagates up-dip along the kink, whereas the along-strike propagating rupture front arrives later but still interacts with the former. We observe large and localized shallow rake rotation at both kinks (Fig. 2c).

## Discussion

In our analysis of four dynamic rupture scenarios of large strike-slip earthquakes with varying source complexity, we find localized rays of elevated  $f_c$  in the vertical components of each event. Albeit path and 3D basin effects, this variability in equivalent near-field corner frequencies is dominated by source effects. The large vertical high-frequency radiation is caused by complex dynamic mechanisms, including shallow dip-slip generated by a rake rotation when the rupture breaks the surface and strong stopping phases due to rupture complexity, for example, at a barrier or a fault kink. The high-amplitude lobes of the P-SV radiation pattern and the directivity effect shape the rays to form a 45° angle to the rupture forward direction.

Our results imply that high- $f_c$  rays correlate with certain characteristic rupture dynamics. The rays often point to locations where dynamic rupture decelerates suddenly, specifically during the breaking of the Earth's surface. Abrupt stopping is usually caused by rupture complexity. For example, dynamic rupture decelerates quickly when tunneling underneath an

orthogonal intersecting fault in the simulations of the 2019 Ridgecrest sequence. Other rupture complexities that can cause localized high-frequency radiation are fault kinks or sudden changes in along-strike fault geometry, as we observe in the dynamic rupture model of the 1992 Landers earthquake at the JVF–KF and the KF–HVF fault intersections. Our findings can provide a physical explanation of observations that fault "misalignment" (Chu *et al.*, 2021) correlates with enhanced high-frequency seismic radiation due to a typically higher degree of geometric complexity, including more intersecting faults and fault kinks.

Near-field corner frequency analysis may help to constrain slip distribution and slip segmentation at depth. Such analysis can also help correlate fault segments with respective subevents in the moment rate release function of large earthquakes. We find that high- $f_c$  rays can indicate locations of surface rupture. Deconvolution of the observed regional ground motions at a station located perpendicular to the rupture direction of the 1992 Landers earthquake shows that surface offsets correlate with the on-fault slip distribution and structural complexity (e.g., Kanamori et al., 1992; Milliner et al., 2015). The moment rate function of the Landers dynamic rupture model shows that it consists of four sharply separated subevents (Fig. 7b, Kagan and Houston, 2005; Vallée and Douet, 2016). Each of these high- $f_c$  rays that we identify can be clearly associated with one of these subevents. Even the weak moment rate subevent corresponding to the Camp Rock fault rupture is clearly detectable in the  $f_c$  distribution. Because this rupture on the Camp Rock fault is dynamically triggered in our dynamic rupture scenario and spatially separated from the other slipping parts of the fault system, its associated spectral contribution includes complete nucleation and stopping phases and superimposes the overall source spectrum with a secondary spectrum with a higher  $f_c$ .

Although our results show that source complexity strongly affects  $f_{c}$  in the near field, the impact of source complexity on far-field corner frequencies, and, thus, Brune-type stressdrop estimates, may also be larger than typically assumed from simpler rupture models (e.g., Madariaga, 1976, Kaneko and Shearer, 2015; Wang and Day, 2017). Circular and elliptical rupture models show a significant azimuthal  $f_c$  variation caused by rupture directivity and nodal plane effects. Figures S7 and S8 show a comparable effect of directivity on the azimuthal  $f_c$ distribution in our Ridgecrest mainshock and Landers earthquake models. However, in addition, directivity effects are overprinted by small-scale complexity. As a result, the relative variability of  $f_c$  values is ~35% smaller compared with the simpler models of Kaneko and Shearer (2014). The standard deviation of  $f_c$  in our models strongly depends on the azimuth and is generally higher in the vertical components.

Liu *et al.* (2023) found that Brune-type corner frequencies of the spectra of the source time functions of complex events correlate best with the corner frequency of that subevent with the highest moment release. They conclude that the Brune stress drop reflects the stress change of the largest asperity. Our observed spatial variability of  $f_c$  in dynamic rupture simulations paints an even more complex picture, identifying dynamic earthquake characteristics as an important source of ground-motion spectra variability. Recent observations align with our findings: Calderoni and Abercrombie (2023) compare stress drops inferred from finite-fault modeling with Brunetype corner frequencies for the  $M_{\rm w}$  6.0 Amatrice and the  $M_{\rm w}$  5.9 Visso events in Italy. They find that high spectral corner frequencies may not be directly associated with high stress drops but rather reflect high-frequency ground motions caused by rupture complexity. Gallovič and Valentová (2020) compare stress-drop estimates inferred from  $f_c$  of the modeled moment rate functions with the on-fault measured value for ~1600 strike-slip dynamic rupture models. They find that  $f_c$ is affected by details of the generally heterogeneous rupture propagation that cannot be attributed to a single stress-drop parameter. Our results highlight the importance of good azimuthal coverage when inferring Brune-type stress drops from corner frequencies (e.g., Kaneko and Shearer, 2015). Future larger-scale dynamic rupture simulations may investigate dynamic source effects also on far-field stress drops. The presented dynamic rupture scenarios lack small-scale dynamic rupture heterogeneity (Taufiqurrahman et al., 2022; Gallovič and Valentová, 2023), which is associated with a depletion of high-frequency content. However, we expect that including smaller scale rupture complexity may not imprint on the frequency ranges that are most relevant for computing  $f_c$  in our dynamic rupture models of relatively large earthquakes. Analyzing much smaller magnitude events is possible but would require a finer model discretization (i.e., a higher computational cost) to sufficiently resolve the higher frequency bands, for example, associated with a higher  $f_c$ .

It will be interesting to further investigate the effects of different 3D velocity models and their uncertainties, particularly in the near-source region. For example, fault damage zones may affect ground motions over large distances and amplify high-frequency radiation in certain directions (Huang *et al.*, 2016; Yeh and Olsen, 2023).

We believe that our results are generally representative of surface-breaking multifault strike-slip events (e.g., Jia *et al.*, 2023). However, it will be more challenging to apply our approach to analyze reverse or normal-faulting events. There, the component separation is more difficult, and the free surface has an asymmetric effect (e.g., Oglesby *et al.*, 1998, 2000; Biemiller *et al.*, 2022). Similarly interesting and challenging would be applying our approach to mixed-faulting multifault events such as the 2016  $M_w$  7.8 Kaikōura earthquake (Ulrich, Gabriel, *et al.*, 2019).

Umeda (1990) introduced the concept of an "earthquake bright spot" as a localized area in the shallow fault region that emits strong high-frequency waves. Specifically, the Landers earthquake fault system kink where the JVF branches into the KF has been identified as an earthquake bright spot (Yamashita and Umeda, 1994), which agrees with our dynamic rupture model analysis, in which it is a prominent source of a ray of elevated  $f_c$ . Yamashita and Umeda (1994) propose that the nucleation and arrest of slip on subsidiary faults cause earthquake bright spots. We find that rake-rotated along-strike surface-breaking rupture fronts that encounter geometric fault complexities can locally cause strong acceleration pulses, which can equally explain the origin of earthquake bright spots without the need for secondary faults.

In addition, tossed-up boulders indicate that coseismic vertical accelerations exceeded gravity during the 1992 Landers earthquake (Yamashita and Umeda, 1994) and similar high vertical accelerations were recorded or inferred for other large strike-slip earthquakes (e.g., Archuleta, 1982; Strasser and Bommer, 2009; Kaiser *et al.*, 2017; Hough *et al.*, 2020). Numerous vertical acceleration recordings of reverse-faulting earthquakes exceeded gravity (e.g., Bilham and England, 2001; Causse *et al.*, 2021), which is not unexpected because the vertical components are affected more strongly by *SH* waves. We demonstrate how complex source mechanisms of surface-rupturing strike-slip events can cause strong vertical acceleration pulses that may locally exceed gravity.

Equivalent near-field corner frequency analysis of the  $M_w$  6.4 Searles Valley model showcases the capability of  $f_c$  variability to track major path effects. A mountain range deflects a high-frequency wave packet and directs seismic energy in an unexpected direction. We find evidence of this deflection in observed waveforms, for example, at station WMF (Fig. 6a–c), where this effect doubles the shaking duration. Such path effects can be relevant for seismic hazard assessment but may be missed in ground-motion models that do not include variability in shaking duration.

Although each presented  $f_c$  distribution map is inferred from more than 1,000,000 virtual stations, important aspects of our findings are equally inferrable from lower resolution analysis, for example, using only 1% of the data (~10,000 virtual stations with a spacing of ~5 km, Fig. S4), which is promising for potential real-world applicability of the method. For example, the six high- $f_c$  rays pointing away from the fault trace and the sharp  $f_c$  increase at the Salton Sea basin in the south and the San Bernardino and Los Angeles basins in the southwest, are still clearly visible in the low-resolution version of the vertical  $f_c$  distribution of the Landers model (Fig. S4). Similarly dense seismic sensor networks are becoming feasible and allow the study of seismic source processes with increasing detail. For example, the LArge-*n* Seismic Survey in Oklahoma (LASSO) experiment deployed more than 1800 vertical-component nodal seismometers covering a 25 km by 32 km region with a station spacing of ~400 m (Dougherty et al., 2019). Trugman et al. (2021) used the LASSO array to investigate the frequency dependence of observed radiation patterns of  $M_{\rm L}$  1.7–2.8 events and found that a strong isotropic

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component at higher frequencies is likely caused by source complexity. DAS can provide linear arrays with a sensor spacing of ~10 m (e.g., Zhan, 2019). Li, Kim, *et al.* (2023) used backprojected DAS data to identify high-frequency subevents of the 2021 Antelope Valley earthquake.

## Conclusions

In this study, we present a detailed analysis of the spatial variability of an equivalent near-field corner frequency  $f_c$  in large strike-slip 3D dynamic rupture simulations. We discover patterns of highly variable  $f_c$  and show that  $f_c$  variability is dominantly controlled by source effects. Rays of locally increased  $f_c$  values radiate outward from the dynamically slipping faults, particularly noticeable in the vertical components. We validate the variability in the distribution of  $f_c$  from the dynamic rupture model with those derived from observed spectra. We use isochrone analysis to show that the radiation of vertical high frequencies often results from rake-rotated surfacebreaking rupture fronts that decelerate suddenly due to source complexities, such as fault heterogeneities or geometric complexity. We observe that the *P*-SV radiation pattern, in combination with the directivity effect, shapes high- $f_c$  rays at a 45° angle to the forward rupture propagation direction. This dynamic source effect can potentially explain observations of high-intensity, impulsive near-field vertical ground motions. The analyses of near-field  $f_c$  distributions can inform on the characteristics of earthquake kinematics and dynamics including rupture directivity, surface rupture, and fault segmentation. We find that path effects additionally imprint on the dynamic rupture equivalent corner frequencies of near-field spectra. For example, we observe a strong deflection of a high- $f_c$  ray along the southern Sierra Nevada mountain range in the  $M_{\rm w}$  6.4 Searles Valley simulation. In conclusion, our findings highlight that the equivalent near-field corner frequency may serve as an insightful ground-motion parameter.  $f_c$  can be inferred from spatially dense, relatively low-frequency ground-motion data sets, thereby offering an approach to directly infer the spectral fingerprints of rupture dynamics from near-field ground motions. Our study has important implications for seismic hazard assessment and offers new avenues for interpreting large array or DAS data to improve our understanding of the dynamics and ground motions of large earthquakes.

## **Data and Resources**

The described complexity of each dynamic rupture earthquake scenario is best illustrated in animations of the dynamic rupture models of the 1992  $M_w$  7.3 Landers earthquake available at https://www.youtube.com/ watch?v=zi19g5Jpp5s, the 2019  $M_w$  6.4 Searles Valley foreshock available at https://www.youtube.com/watch?v=4b\_uhs\_rT\_g, and the 2019  $M_w$  7.1 Ridgecrest mainshock available at https://www.youtube.com/ watch?v=8yP0rcC7n-g. The open-source software package SeisSol is available at https://github.com/SeisSol/SeisSol. All input files that are needed to run the Ridgecrest models are available at Zenodo (https://zenodo.org/record/6842773). The SeisSol branch that was used to run the Ridgecrest models is also archived at https://zenodo.org/ record/7642533. The script that calculates the equivalent near-field corner frequencies from SeisSol's free surface output is provided in the repository available at https://github.com/SeisSol/SeisSol/blob/master/ postprocessing/science/spectral\_corner\_frequency\_from\_surface\_xdmf. py. The script that was used to compute isochrons directly from SeisSol's raw output data are openly available in the SeisSol repository at https://github.com/SeisSol/SeisSol/blob/master/postprocessing/science/ compute\_isochrones.py. The scripts use the external libraries NumPy and SciPy (Harris et al., 2020; Virtanen et al., 2020). Details about the TPV5 benchmark problem are provided on the homepage of the Southern California Earthquake Center (SCEC)/U.S. Geological Survey (USGS) rupture dynamics code verification community effort available at https://strike.scec.org/cvws/tpv5docs.html. All seismic data were downloaded through the Incorporated Research Institutions for Seismology (IRIS) Wilber 3 system available at https://ds.iris.edu/ wilber3/ from the Southern California Seismic Network (CI, California Institute of Technology and U.S. Geological Survey [USGS] Pasadena, 1926). The Python package ObsPy was used to remove the instrument response (Krischer et al., 2015). The other relevant data to Table A1 were available at https://strike.scec.org/cvws/tpv5docs.html. The supplemental material contains eight additional figures. All websites were last accessed in November 2023.

## **Declaration of Competing Interests**

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## Appendix

## 3D dynamic rupture models

The TPV5 U.S. Geological Survey (USGS)/Southern California Earthquake Center (SCEC) dynamic rupture community benchmark (Harris *et al.*, 2009) describes a bilateral strike-slip earthquake in 3D dynamically propagating across a rectangular fault that intersects the free surface in an elastic half-space. The rupture is artificially nucleated in the middle of the fault and then spreads spontaneously in each direction. To the left or right of its center, the model setup includes an asperity and a barrier with elevated or reduced initial shear stresses, which accelerate or decelerate dynamic rupture, respectively. The rupture is forced to stop abruptly at the fault edges. The dynamic model parameters are summarized in Table A1.

Wollherr *et al.* (2019) developed a 3D dynamic rupture model of the 1992  $M_w$  7.3 Landers earthquake that includes

#### TABLE A1

## Summary of the TPV5 Dynamic Rupture Model Parameters (See Data and Resources; Harris *et al.*, 2009)

Symbol	Parameter	Value
$\mu_s$	Static friction	0.677
$\mu_d$	Dynamic friction	0.525
D <sub>c</sub>	Critical slip-weakening distance	0.4 m
Cohesion	Frictional cohesion	0.0 MPa
S <sub>yy</sub>	Stress	120 MPa
$S_{XX}$ , $S_{ZZ}$ , $S_{YZ}$ , $S_{XZ}$	Stress	0 MPa
S <sub>XY</sub>	Stress outside the nucleation zone	70 MPa
	Stress inside the nucleation zone	81.6 MPa
	Stress inside the barrier	62 MPa
	Stress inside the asperity	78 MPa

geometric fault complexity and matches a broad range of regional and local observations, including fault slip, seismic moment release, and ground motions (Fig. 7). The dynamic rupture earthquake model uses a linear slip-weakening friction law, high-resolution topography, 3D velocity structure (CVM-H; Shaw et al., 2015), viscoelastic attenuation, and offfault (visco-)plasticity. Q values are proportional to the S-wave velocity as  $Q_S = 0.05V_S$  and  $Q_P = 2Q_S$  (Graves *et al.*, 2008). The fault system of the Landers dynamic rupture model consists of five vertical subfaults that extend to a depth of 15 km, adapted from fault traces from photometric images (Fleming et al., 1998). The fault system exhibits a strike rotation of  $\sim 30^{\circ}$ , striking toward the north in the southern part and toward the northwest in the northern part. Wollherr et al. (2019) find that assuming a constant maximum principal stress direction inhibits rupture propagation across the fault system. In their setup, the maximum principal stress axis varies smoothly, which is consistent with the regional stress estimates. Dynamic rupture is initiated by gradually reducing the static friction coefficient to its dynamic value within a circular nucleation patch of radius 1.5 km (Bizzarri, 2010). Table A2 provides an overview of all model parameters.

Taufiqurrahman *et al.* (2023) modeled linked foreshockmainshock dynamic rupture scenarios of the 2019 Ridgecrest sequence, the  $M_w$  6.4 Searles Valley foreshock, and the  $M_w$  7.1 Ridgecrest mainshock. Their dynamic rupture scenario assembles earthquake physics with high-quality strong-motion and teleseismic, field mapping, high-rate Global Navigation Satellite Systems (GNSS), and space geodetic foreshock and mainshock data sets of California's largest earthquakes for 20 yr. The initial 3D stress state is inferred from tectonic background loading (Yang and Hauksson, 2013), which is

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## TABLE A2 Summary of the Landers Dynamic Rupture Model Parameters (Adapted from table 1 in Wollherr *et al.*, 2019)

Symbol	Parameter	Value with Units
$\mu_s$	Static friction	0.55 (0.44 at the Emmerson fault and Camp Rock fault)
$\mu_d$	Dynamic friction	0.22
D <sub>c</sub>	Critical slip distance	0.62 m
С	Bulk cohesion	Depth-dependent, good quality rock model of Roten <i>et al.</i> (2017)ranging between 2.5 and 50.0 MPa
$\phi$	Friction angle	0.55
$V_S, V_P$	Shear- and <i>P-</i> wave velocity	3D CVM-H model Shaw et al. (2015)
ρ	Density	3D CVM-H model Shaw et al. (2015)
Q <sub>S</sub> ,Q <sub>P</sub>	Viscoelastic damping parameters	50 V <sub>s</sub> , 2 Q <sub>s</sub>
R	Nucleation patch radius	1.5 km
	Forced nucleation time	0.6 s
R	Relative prestress ratio	0.65
σ2	Principal vertical stress	(2700–1000) kg/m 9.8 abs (depth m)
$\sigma_1, \sigma_3$	Principal horizontal stresses	Amplitudes determined by <i>R</i> and equations (2) and (3) in Wollherr <i>et al.</i> (2019)
dx	Smallest element edge	200 m
p	Polynomial order of accuracy	4

additionally modulated by long-term Coulomb failure stress changes ( $\Delta$ CFS) caused by previous major earthquakes in the eastern California shear zone (Verdecchia and Carena, 2016). The prestress of the mainshock dynamic rupture scenario includes stress changes induced by the foreshock. Although a realistic dynamic rupture scenario of the Ridgecrest mainshock needs to account for the stress changes due to the Searles Valley foreshock, the foreshock does not dynamically trigger the mainshock. The models include viscoelastic attenuation, off-fault plasticity, and a nonvertical quasiorthogonal 3D fault system with four fault segments (Fig. 3). Taufiqurrahman *et al.* (2023) construct the fault system geometry by integrating geological field mapping, geodetic

## TABLE A3

## Rate-and-State Frictional Fault Properties of the Ridgecrest Sequence Models (Adapted from table S2 in Taufiqurrahman *et al.*, 2023)

Parameter	Symbol	Value
Direct-effect parameter	a	0.01-0.02
Evolution-effect parameter	b	0.014
Reference slip rate	V <sub>0</sub>	10 <sup>-6</sup> m/s
Steady-state low-velocity friction coefficient at the slip rate $V_0$	f <sub>0</sub>	0.6
Characteristic slip distance of the state evolution	L	0.2
Full weakened friction coefficient	f <sub>w</sub>	0.1
Initial slip rate	V <sub>ini</sub>	10 <sup>-16</sup> m/s
Weakened slip rate	V <sub>w</sub>	0.1 m/s

Interferometric Synthetic Aperture Radar data, relocated seismicity, and selected focal mechanisms (Carena and Suppe, 2002). The fault system is embedded into a 3D velocity model of southern California (CVM-S4.26; Lee *et al.*, 2014; Small *et al.*, 2017) and intersects high-resolution topography. Q values are coupled to the velocity structure as  $Q_S = 0.1V_S$  and  $Q_P = 1.5Q_S$  (Olsen *et al.*, 2003). Table A3 summarizes the frictional fault properties. Both ruptures are nucleated by imposing shear stress perturbations in spherical nucleation areas with radii of 3.5 km around their respective hypocenters.

All dynamic rupture simulations use the open-source software package SeisSol (see Data and Resources) to solve the problem of spontaneous frictional failure on prescribed faults and nonlinearly coupled seismic wave propagation. SeisSol uses the arbitrary high-order accurate derivative discontinuous Galerkin (ADER-DG) method and employs fully adaptive, unstructured tetrahedral meshes (Dumbser and Käser, 2006; de la Puente et al., 2009; Pelties et al., 2012). Tetrahedral elements enable meshing flexibility and are crucial to incorporate complex and intersecting geometries such as those inherent to the Ridgecrest and Landers fault systems. SeisSol is verified in a variety of dynamic rupture benchmark problems (Pelties et al., 2014; Harris et al., 2018) and is optimized to efficiently exploit high-performance computing infrastructures (e.g., Breuer et al., 2014; Uphoff et al., 2017, Krenz et al., 2021). SeisSol supports high computational efficiency when incorporating elastic, anisotropic, viscoelastic, viscoplastic, and poroelastic rheologies (Uphoff and Bader, 2016; Wollherr et al., 2018; Wolf et al., 2020, 2022). The Landers and Ridgecrest dynamic rupture earthquake scenarios account for off-fault (visco)plasticity and viscoelastic attenuation. Within our here-considered model domains, the seismic wavefield is resolved up to at least 1 Hz in the TPV5 and Landers models and up to 2 Hz in the Ridgecrest dynamic rupture simulations. Synthetic spectra of an underresolved numerical model would deviate from the typical  $\omega^2$  decay (Figs. S5 and S6, Wollherr *et al.*, 2019). The TPV5 dynamic rupture model requires 2000 central processing unit (CPU) hours on the supercomputer Supermuc-NG, the Landers earthquake scenarios require ~100,000 CPU hours on Supermuc Phase-2, and the linked simulation of the Ridgecrest sequence requires 243,000 CPU hours on Supermuc-NG.

## On near-field effects

There exist different approaches to separate far- from near-field effects. The ratio of the distance to the source, R, and the examined seismic wavelength,  $\lambda$ , can determine the

relevance of near-field terms (i.e., static displacements). If  $R/\lambda \gg 1$ , near-field terms are negligible (Madariaga, 2015). In addition, the relevance of source finiteness is considered to be large when the ratio of earthquake rupture duration  $T_R$  and the examined seismic wave period  $T(T_R/T)$  is large (Stein and Wysession, 2003). Our dynamic rupture scenarios include regions where near-field terms are negligible. However, within the analyzed frequency ranges, the waveforms are generally expected to be affected by finite-source effects within the considered model domains.

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