

1 **Three-Dimensional Numerical Modeling of Coseismic**
2 **Atmospheric Dynamics and Ionospheric Responses in**
3 **Slant Total Electron Content Observations**

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13 **Key Points:**

- 14 • Acoustic-gravity wave-driven slant total electron content (sTEC) signals are an-
15 alyzed in terms of amplitude, waveform, and onset time
- 16 • Intricate sTEC signal waveforms result from ionospheric fluctuations measured
17 along lines-of-sight between satellites and receivers
- 18 • High sensitivity of sTEC signals to acoustic-gravity wave source specification pro-
19 vides additional basis for earthquake characterization

Abstract

Despite routine detection of coseismic acoustic-gravity waves (AGWs) in Global Navigation Satellite System (GNSS) total electron content (TEC) observations, models of the earthquake-atmosphere-ionosphere dynamics, essential for validating data-driven studies, remain limited. We present the results of three-dimensional numerical simulations encompassing the entire coupling from Earth’s interior to the ionosphere during the M_w 7.8 2016 Kaikoura earthquake. Incorporating the impact of data/model uncertainties in estimating the ionospheric state, the results show a good agreement between observed and simulated slant TEC (sTEC) signals, assessed through a set of metrics. The signals exhibit intricate waveforms, resulting from the integrated nature of TEC and phase cancellation effects, emphasizing the significance of direct signal comparisons along realistic line-of-sight paths. By conducting simulations based on earthquake representations with kinematic and dynamic source models, the study demonstrates the quantifiable sensitivity of sTEC to AGW source specifications, pointing to their utility in the analysis of coupled dynamics.

Plain Language Summary

Earthquakes launch acoustic and acoustic-gravity waves (AGWs) into the atmosphere, spanning periods from seconds to minutes, that can reach the ionosphere at ~ 100 -400 km altitude. The majority of AGW detections in the ionosphere are performed with the use of GNSS signals collected with ground-based receivers that nowadays comprehensively cover seismically active regions. However, the modeling of earthquake-atmosphere-ionosphere processes together, essential for validating and supporting data-driven studies, remains rare. We present the outcomes of three-dimensional numerical modeling of interconnected processes, spanning from Earth’s interior to the ionosphere. We conducted a case study focused on the 2016 M_w 7.8 earthquake in New Zealand, renowned for its complexity and comprehensive observations of coseismic AGWs recorded with GNSS signals. Our results demonstrate a high level of accuracy of simulated GNSS signals, also revealing the high sensitivity to the chosen earthquake model and the complexity of resulting ionospheric signals, highlighting the necessity of attributing realistic geometries of GNSS TEC observations. The findings highlight the potential for using GNSS signals to investigate coseismic AGWs to infer characteristics of earthquakes.

1 Introduction

Seismically-excited acoustic-gravity waves (AGWs) in the atmosphere serve as sources of detectable ionospheric plasma density fluctuations (Hines, 1960; Blanc, 1985; Tanaka et al., 1984; Ducic et al., 2003). They are routinely detected by measuring delays of Global Navigation Satellite System (GNSS) signals to infer fluctuations in total electron content (TEC), which is directly proportional to the integrated number of electrons along the path between a GNSS satellite and a ground-based receiver (e.g., Parkinson et al., 1995). The distribution of GNSS receivers in seismically active regions and advancements in temporal resolution of measurements, have significantly bolstered the use of TEC for the detection and analysis of coseismic AGWs (Occhipinti et al., 2013; Komjathy et al., 2016; Astafyeva, 2019). The studies rely on the temporal and spatial characteristic variability of TEC signals, including arrival times (Astafyeva & Shults, 2019; Thomas et al., 2018; Sanchez et al., 2023), amplitudes (Cahyadi & Heki, 2014; Manta et al., 2020; Inchin et al., 2021), and shapes (Astafyeva & Heki, 2009a; Bagiya et al., 2023; Brissaud & Astafyeva, 2022), showing promise for enhancing the operational capabilities of systems that monitor AGW fluctuations in the ionosphere (Savastano et al., 2017; Ravanelli et al., 2021; Maletckii & Astafyeva, 2021; Manta et al., 2021; Martire et al., 2023). Under the introduced terminology *AGW*, we include infrasonic (acoustic) waves, which, in addition to

69 propagating by compressional motions of air, are also influenced by buoyant stratifica-
70 tion of the atmosphere at periods close to acoustic cut-off frequency.

71 At the same time, simulations of earthquake-atmosphere-ionosphere processes, es-
72 sential for validating data-driven studies, remain challenging. Firstly, the development
73 of comprehensive earthquake source models is essential and necessitates a thorough con-
74 sideration of the rupture process to address resulting atmospheric dynamics (Astafyeva
75 & Heki, 2009b; Bagiya et al., 2018). Secondly, high-resolution three-dimensional non-
76 linear and compressible atmospheric models are required for simulating AGWs with pe-
77 riods ranging from seconds to minutes (Inchin, Snively, Williamson, et al., 2020). The
78 resolution of AGWs is required over comparatively large regions to cover line-of-sights
79 (LOS) between GNSS satellites and ground-based receivers. Thirdly, the direct model-
80 ing of ionospheric responses to AGWs is also crucial, taking into account potential non-
81 linear behavior and the complexity of plasma responses to neutral gas drivers within am-
82 bient geomagnetic field (Zettergren & Snively, 2015, 2019). Atmospheric and ionospheric
83 simulations must effectively account for background states and winds, which influence
84 AGW propagation and resulting plasma drifts (Drob et al., 2003; McDonald et al., 2012).
85 The scope and complexity of these processes necessitate a comprehensive analysis of the
86 dynamics at every step and in every system.

87 The magnitude 7.8 Kaikoura earthquake struck the South Island of New Zealand
88 on November 13, 2016 $T_0=11:02:56$ UT (11/14/2016, 00:02:56 local time) and resulted
89 in more than 20 fault segments ruptured, including some previously unknown or con-
90 sidered inactive. Despite the availability of various geophysical datasets, the complete
91 understanding of its rupture evolution remains elusive, positioning this earthquake as
92 one of the most intricate records to date (Kaiser et al., 2017; Hamling et al., 2017). De-
93 spite this, the ionospheric responses to coseismic AGWs were measured by a substan-
94 tial number of multi-GNSS receivers across New Zealand. These detections offered an
95 opportunity to investigate and quantify coseismic processes for an inland earthquake to-
96 gether with ionosphere responses and to propose new techniques for earthquake source
97 characterization (Bagiya et al., 2018; Lee et al., 2018; Zedek et al., 2021; Inchin et al.,
98 2021).

99 We report new results leveraging our fully-3D modeling approach for simulating
100 earthquake-atmosphere-ionosphere coupling processes, applied to the M_w 7.8 Kaikoura
101 earthquake and its associated sTEC signals. We investigate the structure of electron den-
102 sity fluctuations along LOS and the resulting sTEC signals and assess the impacts of un-
103 certainties in estimating background ionospheric states on them. In addition to simu-
104 lations utilizing the earthquake’s kinematic source model, we here compare to simula-
105 tions with a multi-fault dynamic rupture earthquake source model.

106 2 Methodology

107 We conducted seismic wave propagation simulations with the specification of kine-
108 matic and dynamic earthquake source models. The first corresponds to the kinematic
109 source model of Inchin et al. (2021), constrained by strong-motion, InSAR, Global Po-
110 sitioning System (GPS), vertical coastal uplift and tsunami data, and was used to ini-
111 tialize a SPEC-FEM3D simulation (Komatitsch & Vilotte, 1998; Komatitsch & Tromp,
112 2002). For the second, coupled dynamic source model and wave propagation simulation
113 was conducted with the SeisSol software (Dumbser & Käser, 2006; Pelties et al., 2013;
114 Breuer et al., 2014; Uphoff et al., 2017) with dynamic source model described in Ulrich
115 et al. (2019). Coupling with nonlinear and compressible neutral atmosphere model MAGIC3D
116 was made through the transfer of vertical momentum at the surface (Inchin, Snively, Zetter-
117 gren, et al., 2020). MAGIC3D simulations were configured with a spatial resolution of
118 500 m in horizontal and 250 m in vertical directions. Atmospheric stratification and winds
119 were based on global empirical models NRLMSISE-00 and HWM-14 (Picone et al., 2002;

120 Drob et al., 2015), and covered the heights from the surface to 500 km, with $\sim 9 \times 17.7^\circ$
 121 in meridional and zonal directions. Geomagnetic indexes Kp and Dst during the events
 122 were 3 and -20 nT, respectively. The output of the MAGIC3D simulations, including per-
 123 turbations in major gas species densities, temperature, and fluid velocities, served as drivers
 124 in the three-dimensional ionospheric model GEMINI3D. The basis for MAGIC3D and
 125 GEMINI3D are described in Zettergren and Snively (2015).

126 GNSS TEC observations were calculated using software developed at the Jet Propul-
 127 sion Laboratory gnsstec.py (JPL New Technology Report #52034, Bertiger et al. (2020))
 128 and GIM (Mannucci et al., 1998). We utilized raw GPS and GLONASS navigation and
 129 observation data at a sampling rate of 1 Hz in Receiver Independent Exchange Format
 130 (RINEX). For observations, the height of 300 km was specified as ionospheric shell layer
 131 to calculate ionospheric pierce point (IPP) positions and the absolute vTEC was esti-
 132 mated using a Single Layer Mapping function. Model synthesized sTEC signals were cal-
 133 culated from the integration of electron densities (n_e), based on the outputs of n_e from
 134 GEMINI3D simulations. To compare measured and simulated sTEC signals along tem-
 135 porally and spatially varying LOS, we applied a Butterworth filter with a fourth-order
 136 and a window of 30-600 sec. To obtain simulated n_e perturbation fields, we performed
 137 GEMINI3D simulation excluding AGWs, and subtracted fields of n_e from AGW-driven
 138 run.

139 3 Results

140 3.1 Ionospheric responses to coseismic AGWs

141 The results of seismic wave propagation simulations with a kinematic source model
 142 and atmospheric dynamics were presented by Inchin et al. (2021), whereas here we fo-
 143 cus on fully-3D ionospheric plasma responses to AGWs and sTEC signals. During the
 144 local night-time of the event, the absolute vTEC exhibited values ranging between 6-14
 145 TEC units (TECu) across New Zealand (Figure 1c). While a broad positive gradient of
 146 vTEC is evident from south to north, the observations reveal intricate variations in vTEC,
 147 potentially attributable to ionospheric disturbances of diverse origins. To address the
 148 uncertainty in estimation of absolute vTEC, expected to be at the level \pm several TECu
 149 (Ren et al., 2019; Wielgosz et al., 2021; Chen et al., 2020), and its role in determining
 150 AGW signals in sTEC (~ 0.02 - 0.2 TECu), we conducted two GEMINI3D simulations cor-
 151 responding to the background ionospheric conditions at the time of the earthquake T_0
 152 and T_0 -30 min, but with the same seismic wave propagation and AGW simulation in-
 153 puts with kinematic source model, referred to as Sim #1 and Sim #2. Figure 1a,b de-
 154 picts the absolute vTEC from these simulations. Simulated vTEC ranges from ~ 5 -7 TECu
 155 at the south to ~ 11 -14 TECu over the Northern Island, giving difference between the
 156 simulations of 2-5 TECu over the numerical domain. Figure 1d,e illustrate n_e fields from
 157 Sim #1 along the meridional and zonal directions with altitudes, respectively, sliced over
 158 the center of GEMINI3D domain. The electron density peak altitude (hmF2) from sim-
 159 ulations is at ~ 300 km, reaching values of $5.5 \times 10^{11} \text{ m}^{-3}$.

160 Figure 2a-d illustrate the snapshots of simulated sTEC fluctuations, assuming zenith-
 161 looking LOSs. The leading fluctuations, surpassing the typical noise level of TEC at ~ 0.01 -
 162 0.02 TECu, become discernible ~ 10 min after T_0 . The time required for the rupture prop-
 163 agation spans over ~ 90 sec, with the most pronounced AGWs being generated ~ 60 -80
 164 sec after the rupture initiation (Inchin et al., 2021). The leading fluctuations are slightly
 165 inclined towards the northeast, aligning with the direction of rupture propagation. They
 166 arise from n_e perturbations occurring at altitudes of ~ 230 -250 km, revealing plasma drifts
 167 not fully aligned with magnetic field lines and influenced by larger neutral-ion collision
 168 frequency at these altitudes. The strongest sTEC fluctuations, in this LOS geometry,
 169 are simulated over the Cook Strait, with the positive phase reaching the area ~ 12 min

170 after T_0 . The dominant following plasma drifts are primarily aligned with magnetic field
 171 lines and evolve equatorward (Figure 2c,d).

172 Figure 2e,f display maximum sTEC fluctuations (in LOS geometry as in panels a-
 173 d) and neutral major gas temperature perturbations (their moduli) at 300 km altitude.
 174 The strongest AGWs are found to the north and northeast from the epicenter, arising
 175 from the northeastward propagation of the rupture and focusing of AGWs. Concurrently,
 176 the strongest sTEC fluctuations, up to 0.26 TECu, are observed over the Cook Strait.
 177 The fluctuations to the west and south from the epicenter, as well as offshore to the east,
 178 also exhibit amplitudes higher than TEC noise level, in the range of ~ 0.02 - 0.08 TECu.
 179 The disparities between the fields of simulated sTEC signals and AGW-driven fluctu-
 180 ations highlight the significance of the alignment of plasma drifts driven by AGWs with
 181 magnetic field, exhibiting dominant equatorward motion, even in the present of large am-
 182 plitude dynamics in the neutral gas (Rolland et al., 2013; Zettergren & Snively, 2015;
 183 Bagiya et al., 2017).

184 Simulated n_e fluctuations for six satellite-station pairs along their actual LOSs with
 185 time are presented in top panels of Figure 2g-l. Their Y axes are altitudes along LOSs.
 186 In the corresponding bottom panels, we show the resultant sTEC signals (black lines)
 187 and the altitude at which n_e fluctuations contribute the most to sTEC signals (red lines).
 188 The onset time of sTEC signals corresponds to altitudes ~ 230 - 260 km, depending on the
 189 elevation angle and positioning of LOS. This suggests that sTEC signals are sensitive
 190 to AGW-driven fluctuations at altitudes significantly lower than hmF2. The complex-
 191 ity of n_e fluctuations along the LOS demonstrates the fact that they, and thus sTEC sig-
 192 nals, do not originate from a single, fixed altitude. Instead, this altitude varies in accor-
 193 dance with the evolving plasma drifts over time. While the initial fluctuations in sTEC
 194 may arise from n_e fluctuations contributing at lower altitudes, the peak amplitudes of
 195 these signals can result from heights close to hmF2 or higher at 400-500 km.

196 The nature of sTEC, which involves integrating n_e along the LOS, can introduce
 197 complexities that lead to the potential cancellation of otherwise detectable fluctuations.
 198 This is demonstrated in Figure 2i,l, where the initial positive-phase fluctuations (top pan-
 199 els), although present, contribute minimally to the resulting sTEC signals (bottom pan-
 200 els). Subsequent negative-phase fluctuations dominate in contribution to sTEC, ultimately
 201 resulting in an initial negative phase in signals. The phase-cancellation effect may lead
 202 to signals falling below the threshold of detectability, as demonstrated for the GPS51-
 203 HANM pair. This behavior of n_e fluctuations implies apparent delayed detectability of
 204 sTEC when observed with unsuitable LOS. Likewise, the period and shape of these sig-
 205 nals vary depending the alignment of plasma drifts relative to the LOS.

206 3.2 Comparison of observed and synthetic sTEC signals

207 Figure 3 provides a comparison between observed and simulated sTEC signals. The
 208 focus of our analysis lies within observations taken over Cook Strait. The other groups
 209 of observations originated from areas west of the epicenter, spanning over North Island
 210 of New Zealand, and over the ocean to the east of the epicenter. Although still finding
 211 a sufficient level of agreement with observations, we omitted most signals originating to
 212 the south of South Island, as they consistently exhibited signal amplitudes below expected
 213 TEC noise level (~ 0.01 - 0.02 TECu). Simulated sTEC signals in Figure 3 are calculated
 214 along actual LOSs, i.e., in the same geometry as they were observed during the event.

215 First, we find that the variability of the background ionospheric state between Sim
 216 #1 and Sim #2 does not translate into a notable difference in simulated sTEC signals
 217 and neither of the simulations outperformed when compared with the observations. We
 218 expect that the presented uncertainty associated with absolute $\sqrt{\text{TEC}}$ may not neces-
 219 sarily be a source of error when simulating sTEC signals driven by AGWs. However, we
 220 expect that larger discrepancies in absolute $\sqrt{\text{TEC}}$ or variations in the ionospheric lay-

ering unrelated to the event may lead to more significant differences in simulated sTEC fluctuations.

The highest level of agreement of simulated and observed sTEC signals is over Cook Strait with a similar level of concordance to the west and northwest of the epicenter. A common trend of smaller amplitudes in the simulated signals over Northern Island is noted. Here, despite closely matching the shapes of the signals and onset times, simulated sTEC consistently exhibit $\sim 50\%$ lower amplitudes. It is unlikely that the underestimation of absolute vTEC is the primary cause of such differences. This discrepancy may be due to the inaccuracies of 3D velocity structure, especially in the offshore region, assumed in the earthquake model or under-resolving related AGW dynamics in the atmosphere. Separately, analyzing sTEC signals to the east of the epicenter, we find that their amplitudes are effectively captured by simulations, but they appear ~ 20 sec earlier in time than the observed ones. We attribute this to a potential lack of constraints on rupture propagation offshore, which is less evident based on available geodetic data. Lastly, Figure 3 presents a comparison of signals located to the south of the epicenter, which mostly agree, but exhibit limited utility due to low signal-to-noise ratio. Understanding the causes of sTEC discrepancies for some satellite-station pairs to the north and east require further in-depth parametric investigation.

To quantify the differences between simulated and observed sTEC, we implemented a set of metrics, including the time of flight (TOF), maximum and minimum amplitudes, the duration of pulses, and the temporal track cross-correlation of signals. An example of metrics estimation is presented for pair GPS51-LEVN in Figure 3 and full metric analysis is provided in the Supplemental Materials. The TOF error is determined as the difference between the observed and simulated sTEC fluctuation onset times. As the onset time, we identify the point at which the derivative of the sTEC signal exceeds the trend four times. The errors in amplitude and the duration are calculated for the main pulse, which falls between signal onset time and the point where the N-shaped pulse crosses zero amplitude from negative. The cross-correlation coefficient, providing a measure of observed and synthetic signal linear dependence, is calculated over a period from 120 sec before the TOE to the last simulated time step. The selected subset of 92 satellite-station pairs is focused on clearly identifiable signals of AGWs in sTEC, where metrics could be calculated automatically. The underresolved signals to the north of the North Island, east to the Ocean and south (with sTEC signals close or below the TEC noise of ~ 0.01 - 0.02 TECu) are excluded from the analysis.

On average, the metric errors are as follows: ~ 15 sec for TOF, 10.4% for the duration of the pulse, and 12.2% for the temporal track cross-correlation of signals and 17.9% for the maximum and 20.2% for the minimum amplitudes of the pulse. We find relatively small error in the TOF constituting ~ 15 sec. This error is significantly smaller than the time of AGW arrival from the ground of 600 sec, on average (i.e., $Onset_{obs} - T_0$ sec, where $Onset_{obs}$ is observed sTEC fluctuation onset time), implying sufficiently accurate timing of the source model and good estimation of atmospheric speeds of sound and ionospheric fluctuation altitudes relative to layers. Similarly, we find favorable agreement for the temporal cross-correlation of signals and the period of pulses. The error in pulse duration, ~ 30 sec, is relatively small compared to the total period of the signals, which ranges from ~ 300 - 480 sec, implying reasonable constraint on the source spectrum as well as timing considerations. We find higher levels of errors in the amplitudes of simulated fluctuations, which are found to be the most challenging to replicate, but note that these errors (~ 0.01 - 0.04 TECu) are close to the noise level of TEC observations themselves.

3.3 Kinematic vs dynamic earthquake source model

We performed a set of simulations using the 3D dynamic rupture (e.g, Harris et al., 2018) earthquake source model proposed by Ulrich et al. (2019), referenced as Sim

#3 below. The advantage of dynamic source modeling compared to kinematic models is to account for the physics of spontaneous rupture nucleation, propagation and arrest, which, while more complex, can help to address the problems of non-uniqueness of solutions based on purely data-driven source inversion techniques (e.g., Taufiqurrahman et al., 2023; Jia et al., 2023). Thus, the dynamic model, although less-tuned to describe the observations, serves as a tool for understanding the physics underlying rupture progression, which is especially important for complex earthquakes. Additionally, the ruptured faults and the segment sequence in dynamic model by Ulrich et al. (2019) differs from the kinematic source model by Inchin et al. (2021). The background state of the ionosphere in Sim #3 is specified from Sim #1.

Figure 4a,b illustrates the comparison of maximum absolute vertical velocities at the Earth surface from Sim #1 and Sim #3. The amplitudes are higher in Sim #3 than those simulated with kinematic source model (Sim #1), varying to 3 times in some areas. Related to Sim #3 simulation revealed that AGW amplitudes reach values of 369 m/s of the leading shock and -760 m/s of the tail shock of N-wave at 300 km altitude, exceeding the values from Sim #1 to $\sim 90\%$. For comparison, Figure 4c demonstrates Sim #3 maximum temperature perturbations at 300 km altitude, which peak at 321 K and are $\sim 50\%$ larger than in Sim #1.

Although Sim #3 results in stronger AGWs in the atmosphere than Sim #1, the possibility to infer these differences based on sTEC is yet not clear. Thus, Figure 4d shows sTEC signals from Sim #3 compared with sTEC observations and results of Sim #1. We find markedly stronger sTEC fluctuations in Sim #3, exceeding the amplitudes of observed signals to $\sim 70\text{-}100\%$. A common earlier onset times of signals of $\sim 40\text{-}50$ sec is also evident in Sim #3. This points to the importance of a nonlinear evolution of AGWs to acoustic shock N-waves with height, which then lengthen and exhibit speeds of its leading shock fronts faster than local speed of sound. Likewise, the steepness of the signal is more pronounced in Sim #3 than found in observations or in Sim #1, highlighting the nonlinear evolution of AGWs. Such disagreements between observed and simulated signals is found for practically all sTEC signals (additional figures are provided in the SM) in this case. Thus, the dynamic source model would require additional ingredients to fully capture surface vertical motions (e.g., Kaneko & Goto, 2022; Schliwa & Gabriel, 2024), potentially including GNSS TEC signals of coseismic AGWs as novel constraints.

4 Discussion and Conclusion

We presented the results of novel 3D direct numerical simulations, encompassing the chain of dynamics extending from Earth’s interior and surface, to the atmosphere and to the ionosphere in response to the 2016 M_w 7.8 Kaikoura earthquake. They have enabled us to conduct a comparison between observed and simulated GNSS sTEC signals, considering variations in LOS paths and thus delving into the intricacies of sTEC signals. Our findings highlight that sTEC signal shapes provide a direct representation of the evolution of AGWs even though the structure of the signals is significantly influenced by the integration of electron density fluctuations along the LOS. The geometric phase-cancellation effect can result in the attenuation of AGW-driven fluctuations in sTEC signals below the detectability threshold, making it challenging to accurately determine signal onset times just relying on data. The results also suggest dominant sTEC signal components originating from different altitudes, above or below the peak of electron density. This questions the common practice of using a fixed IPP height to localize sTEC fluctuations, which are particularly relevant in the context of GNSS TEC observations with low elevation angles, when estimated IPP positions change rapidly. The findings highlight that direct comparisons of simulated and observed sTEC signals along realistic LOS can reduce ambiguity and improve fidelity.

322 The results demonstrated a high level of agreement between observed and simu-
 323 lated sTEC signals utilizing a kinematic source model, reinforcing the appropriateness
 324 of this simulation approach and model specifications for constraining surface motion that
 325 drives AGWs. The set of metrics shows promise for applications in the analysis of other
 326 seismic events. At the same time, simulations initialized with the dynamic source model
 327 find sTEC signal differences reflecting the presence of higher vertical velocities (than sim-
 328 ulated with kinematic slip model) at the Earth’s surface that act as sources of AGWs.
 329 This further highlights the opportunity to employ sTEC signals for constraining surface
 330 dynamics during seismic events and to enhance earthquake source models and their val-
 331 idation. Results reinforce the importance of using a large number of observations for the
 332 analysis and validation of observational and simulation results, making sTEC particu-
 333 larly attractive to investigate spatially resolved AGW signals in the ionosphere that pro-
 334 vide insight into their source geometries and evolutions.

335 Open Research

336 The SPECfEM3D software is preserved at [https://geodynamics.org/resources/
 337 specfem3dcartesian](https://geodynamics.org/resources/specfem3dcartesian), available via the GPL 3 license. The open-source software Seis-
 338 Sol is publicly available: <https://github.com/SeisSol/SeisSol> with BSD 3-Clause
 339 Licence. GEMINI3D model is available through <https://github.com/gemini3d/gemini3d>
 340 (Zettergren & Hirsch, 2024) with Apache-2.0 license. GNSS TEC observations used for
 341 the investigation of travelling ionospheric disturbances in the study are available at GeoNet
 342 Aotearoa New Zealand Continuous GNSS Network AWS Open Data access mechanism
 343 <https://www.geonet.org.nz/data/access/aws> with public access.

344 Conflict of Interest Statement

345 The authors declare no conflicts of interest relevant to this study.

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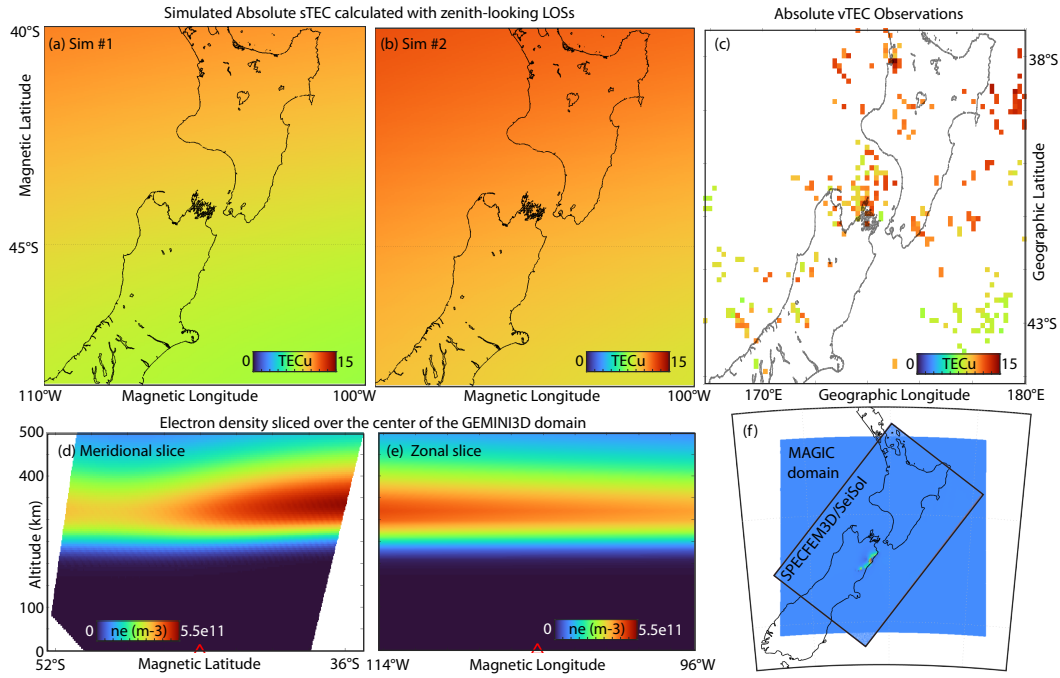
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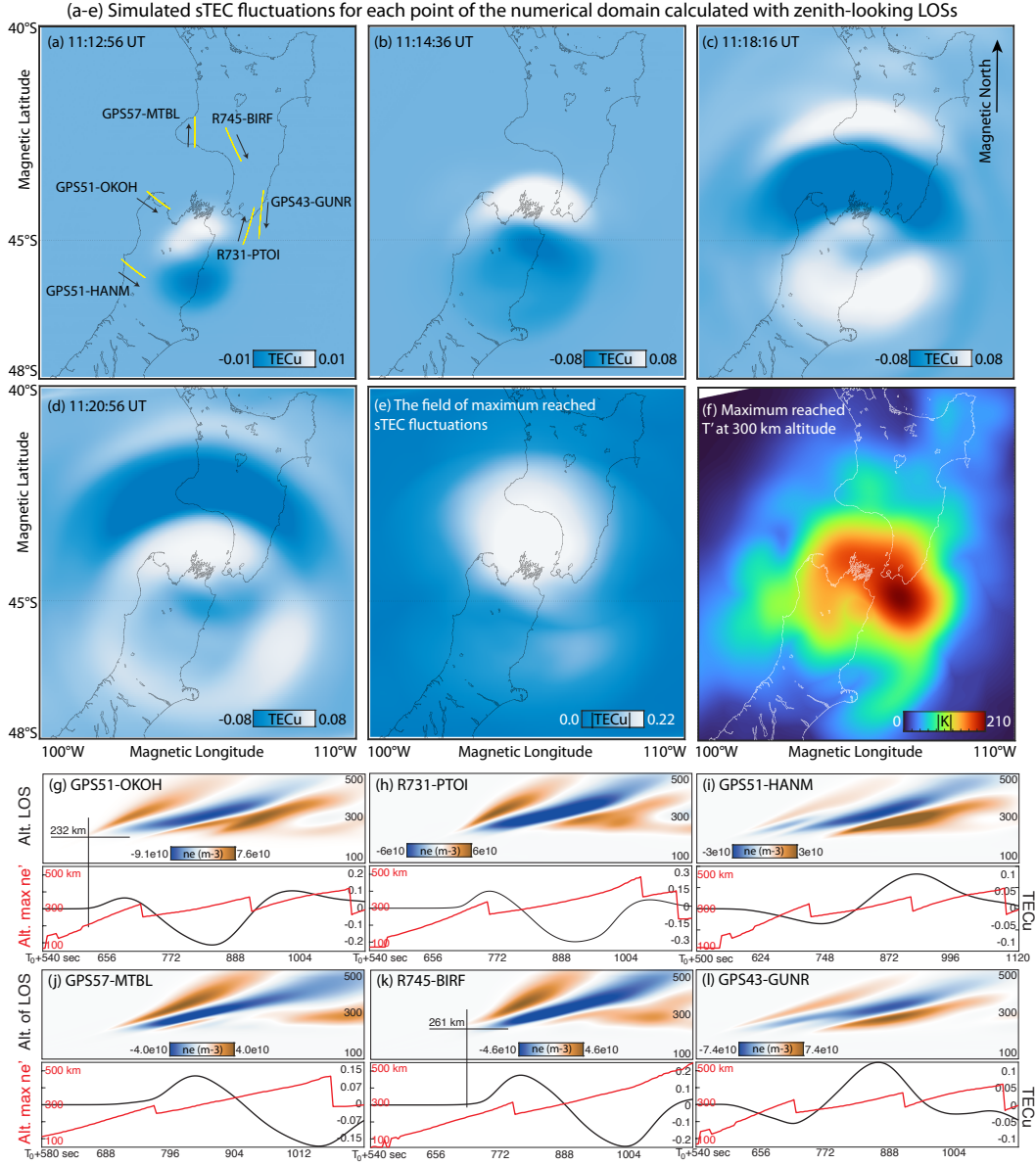
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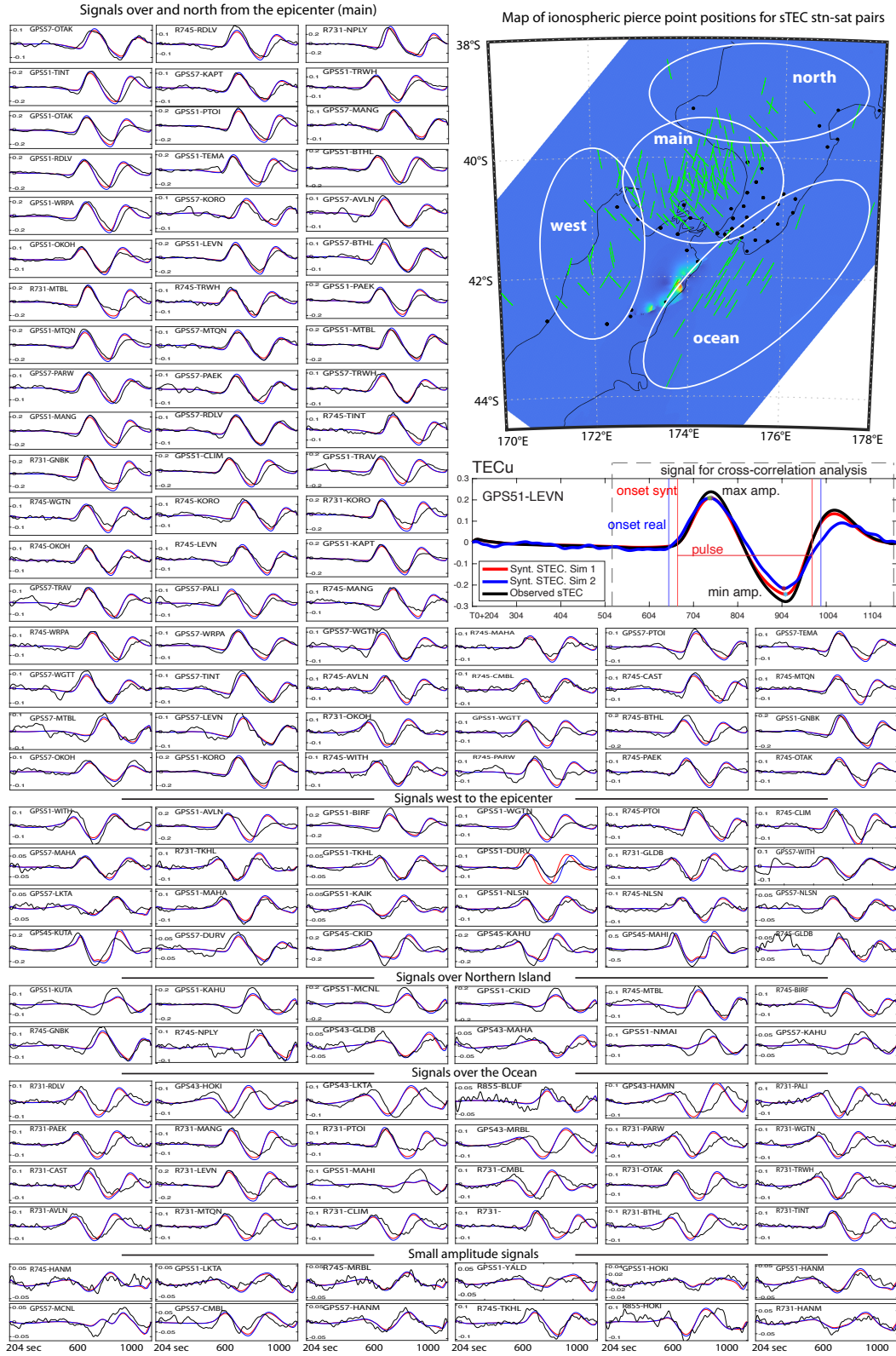
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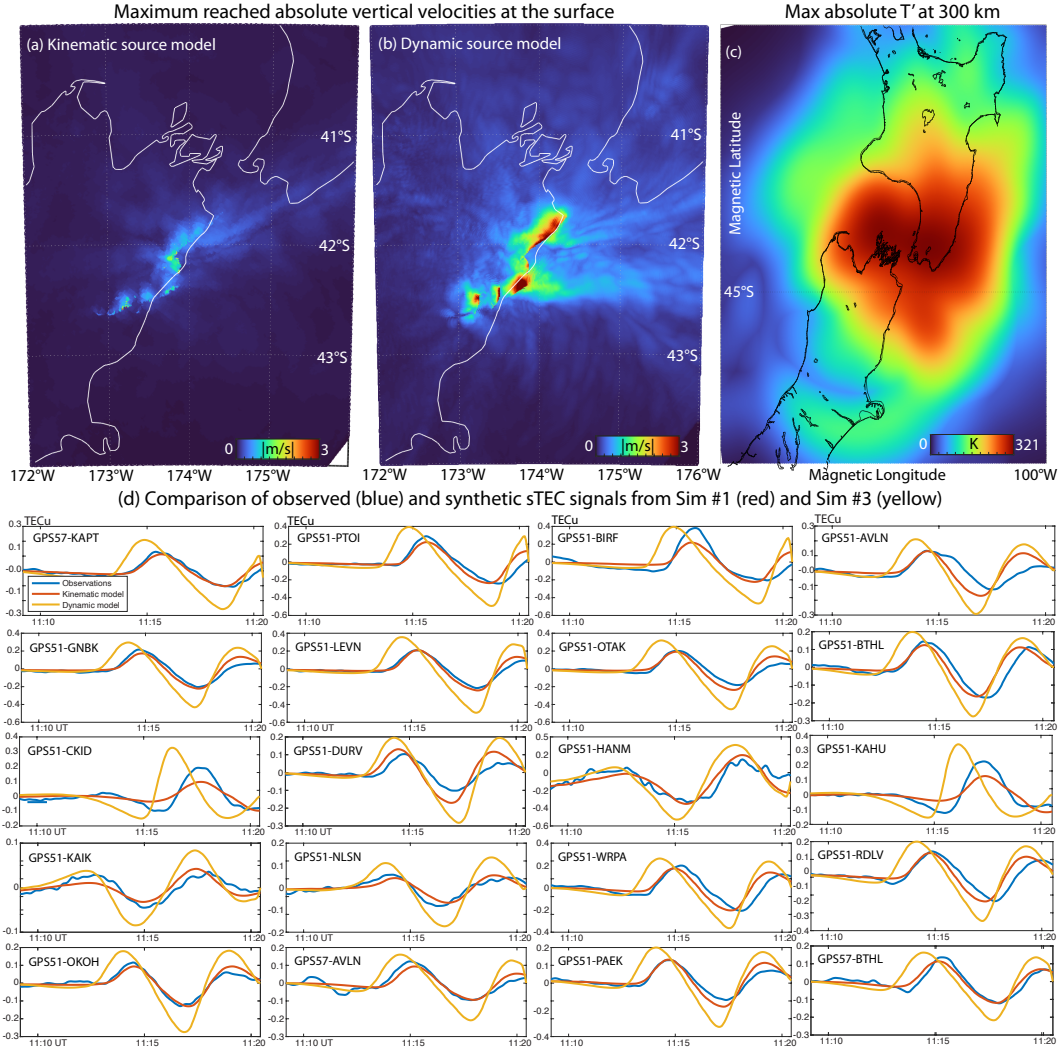
551 **Figure 1.** Absolute simulated sTEC calculated with zenith-looking LOSs at (a) 11:02:56
 552 UT (Sim #1) and (b) 10:32:56 UT (Sim #2). (c) Observations of absolute vTEC at 11:00 UT.
 553 (d,e) Meridional and zonal slices of simulated electron density at 11:02:56 UT. (f) Schematic
 554 representation of maximum vertical velocities at the surface relative to the MAGIC3D numerical
 555 domains.



556 **Figure 2.** (a-d) The snapshots of simulated sTEC fluctuations calculated for each point of
 557 the numerical domain with zenith-looking LOSs at four epochs and (e) the field of their maxi-
 558 mum values (moduli) calculated over the whole time of simulation. (f) Maximum neutral major
 559 gas temperature perturbations (moduli) at 300 km altitude calculated over the whole time of
 560 simulatio. (g-l) Electron density (n_e) fluctuations over the time along realistically spatially and
 561 temporally varying LOSs and resulting sTEC signals (black lines) and the altitudes of maximum
 562 n_e fluctuations (red lines). The IPP positions for satellite-station pairs in panels g-l are shown in
 563 panel a with yellow lines for 20 min from T_0 .



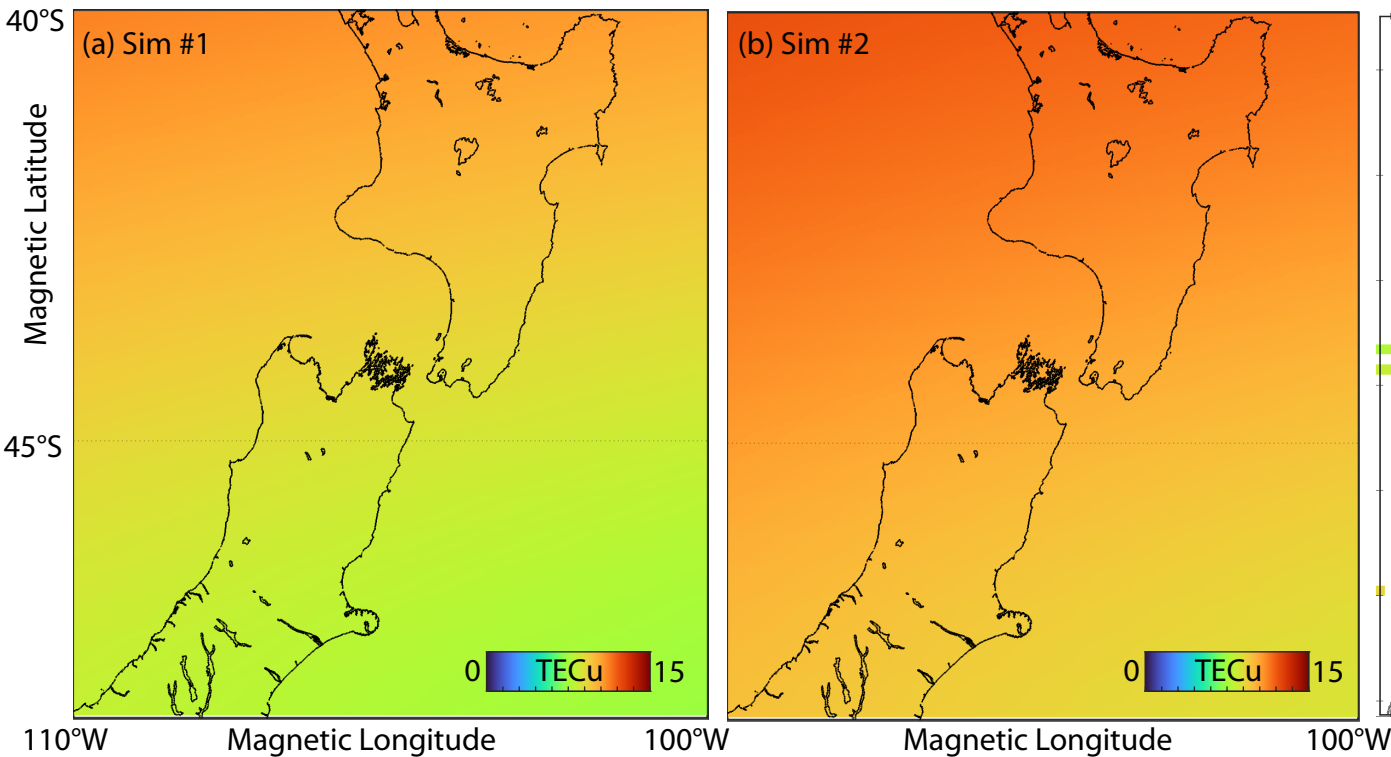
564 **Figure 3.** The comparison of observed (black lines) and simulated sTEC signals from Sim
 565 #1 (red lines) and Sim #2 (blue lines). Simulated sTEC signals are calculated along temporally
 566 and spatially varying LOSs, as measured during the event. Metrics analysis is presented for pair
 567 GPS51-LEVN. The time window from T_0+204 to T_0+1164 sec is chosen for all sTEC time series
 568 demonstrated. The map demonstrates IPP positions of observations. The elongated southwest-
 569 northeast rectangle illustrates final vertical displacements from Sim #1.



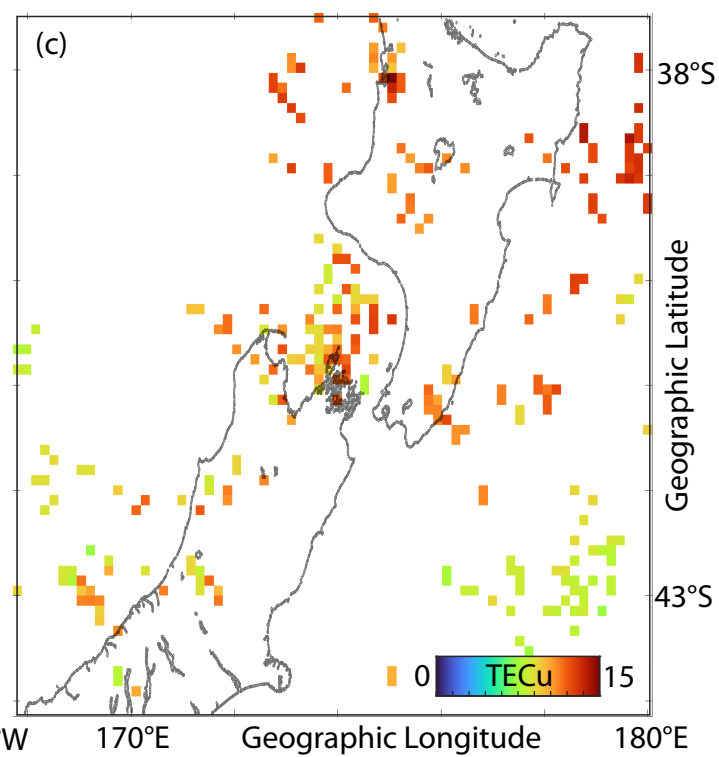
570 **Figure 4.** Maximum vertical velocities reached at the Earth's surface calculated based on the
 571 (a) kinematic source model (Sim #1) and (b) dynamic source model (Sim #2). (c) Maximum
 572 absolute temperature perturbations at 300 km altitude from simulation with dynamic source
 573 model. (d) Comparison of sTEC signals as observed (blue lines), derived from Sim #1 (red lines)
 574 and Sim #3 (yellow lines).

Figure 1.

Simulated Absolute sTEC calculated with zenith-looking LOSs



Absolute vTEC Observations



Electron density sliced over the center of the GEMINI3D domain

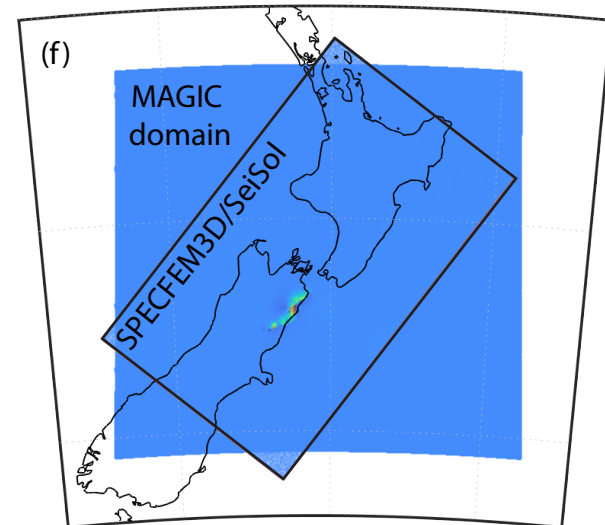
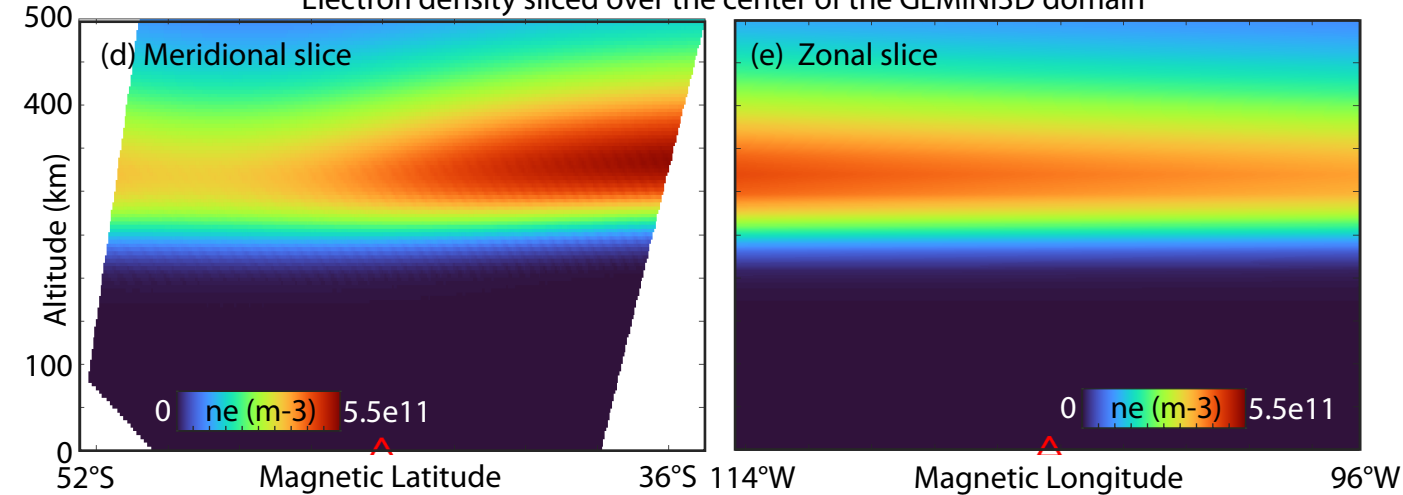


Figure 2.

(a-e) Simulated sTEC fluctuations for each point of the numerical domain calculated with zenith-looking LOS

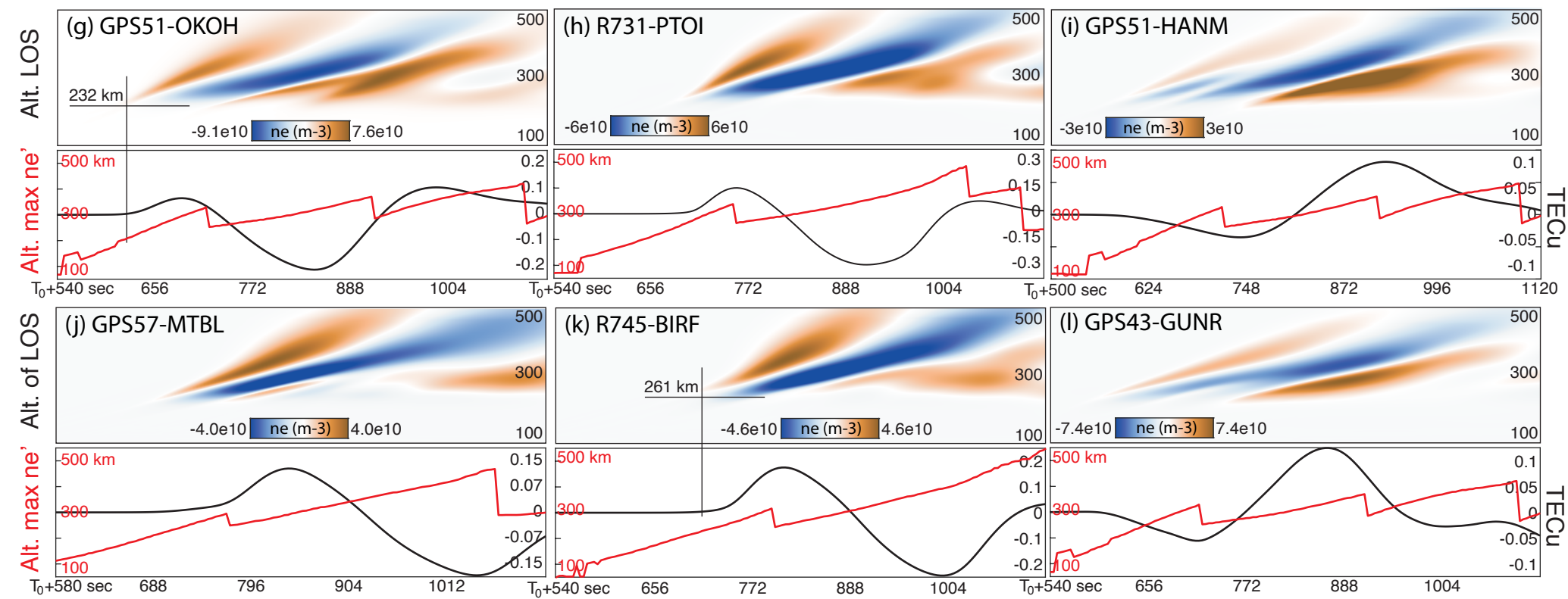
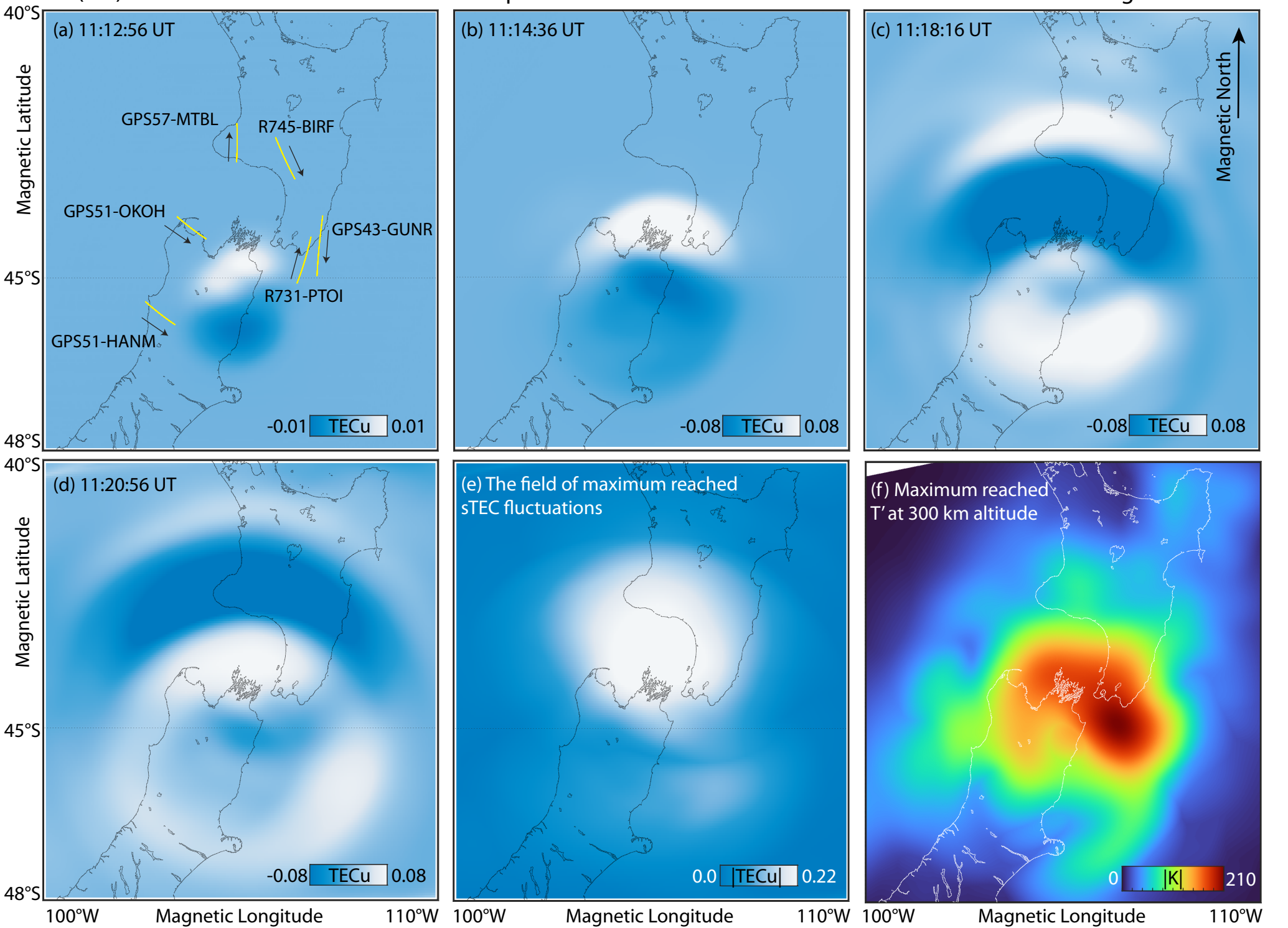
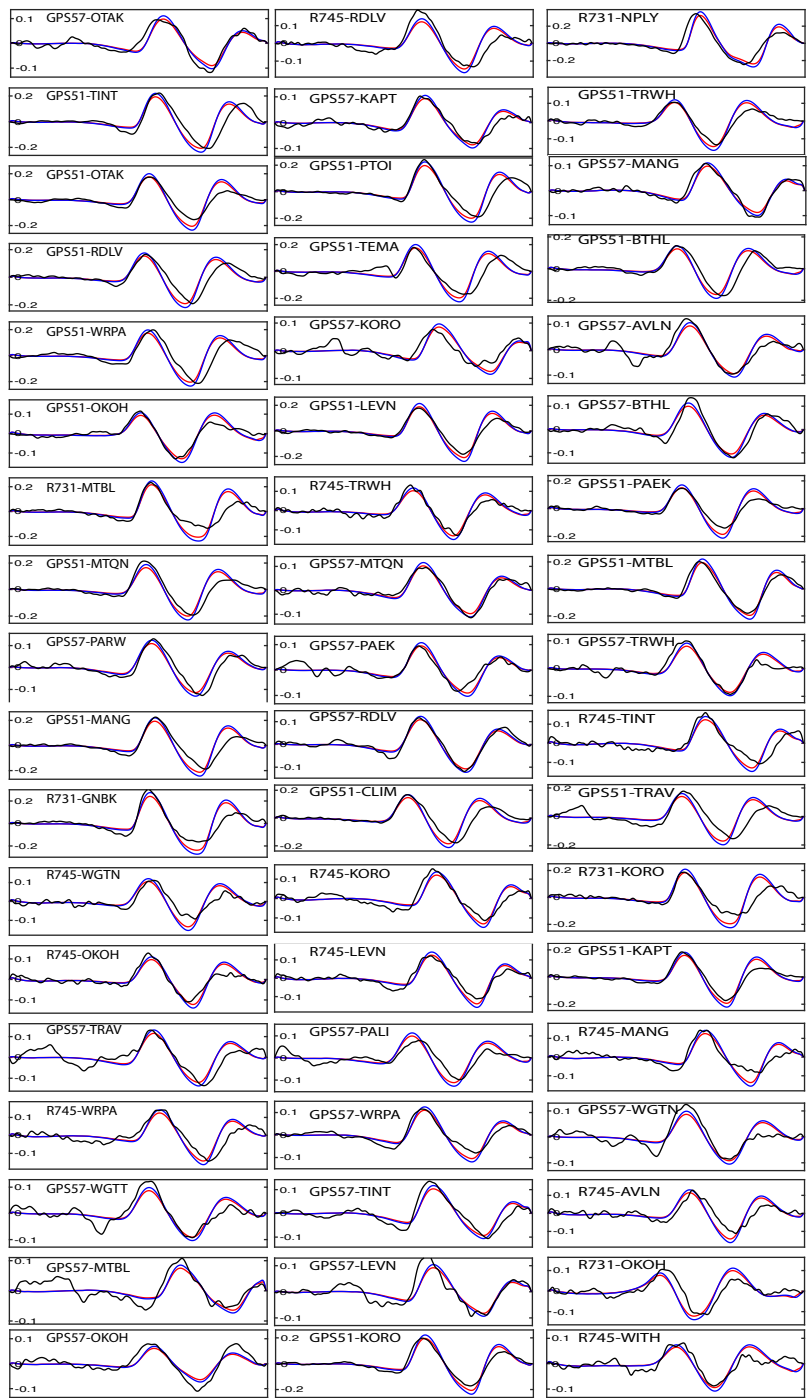
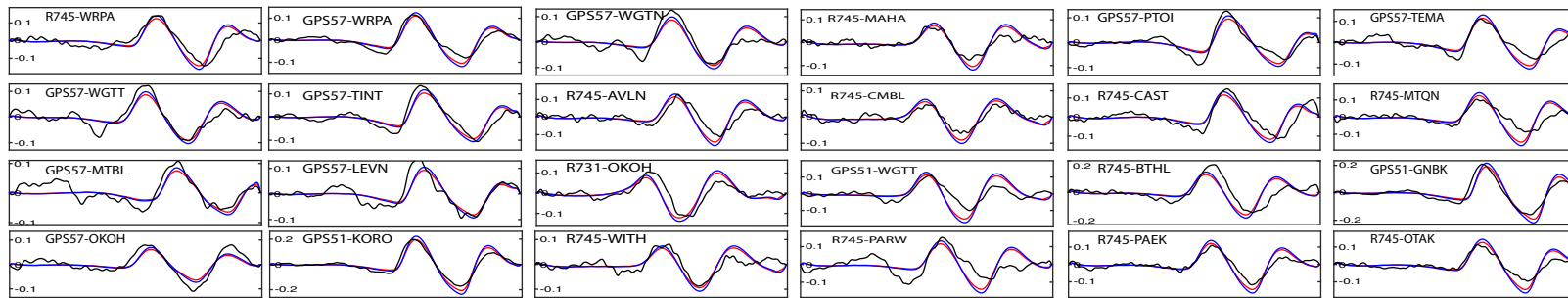
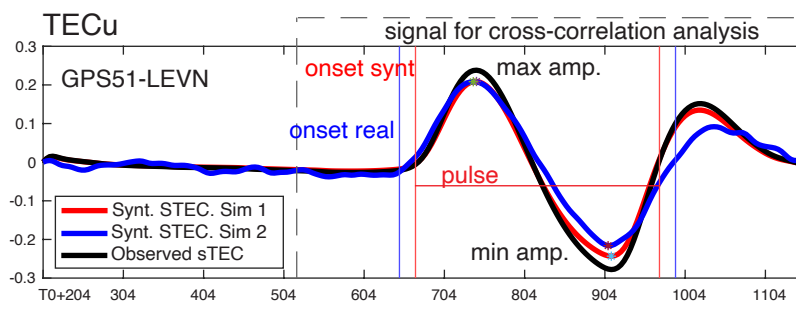
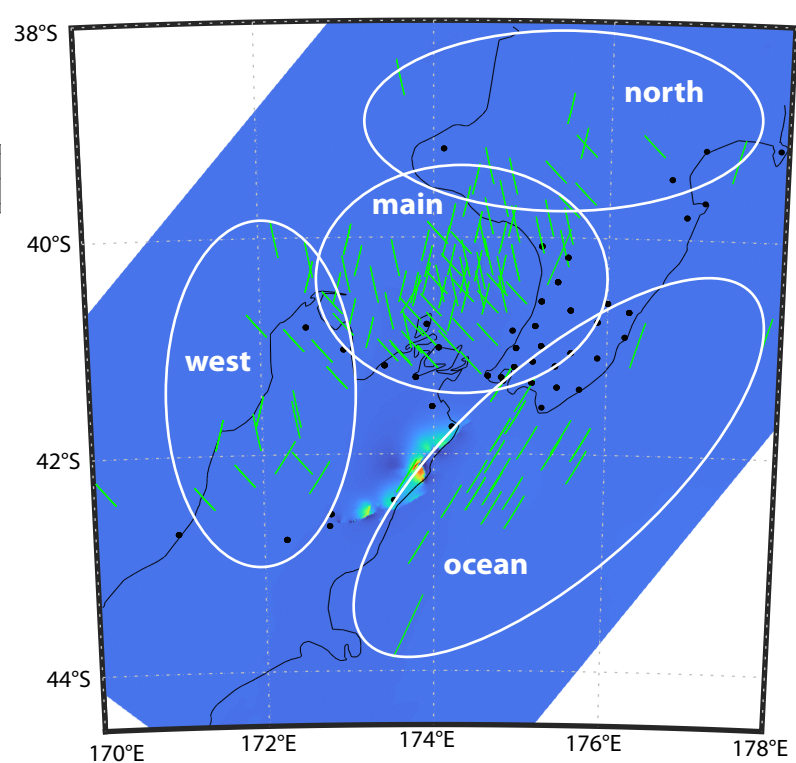


Figure 3.

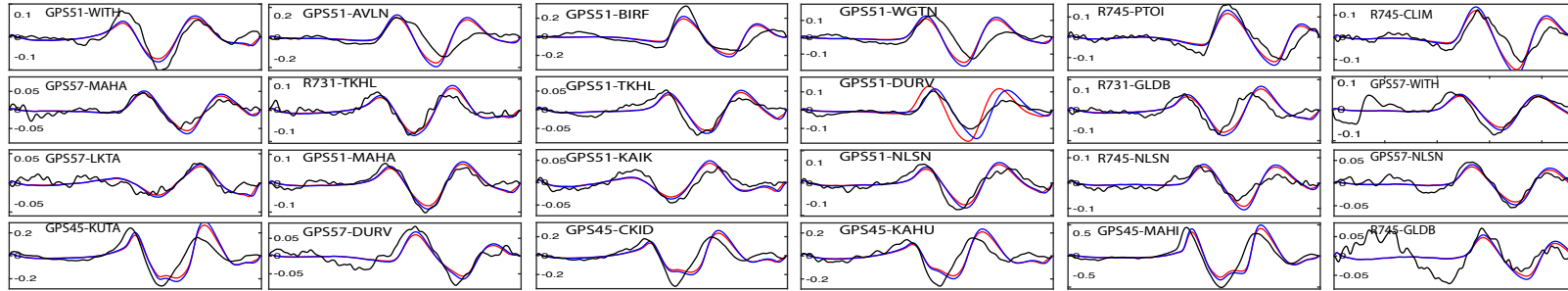
Signals over and north from the epicenter (main)



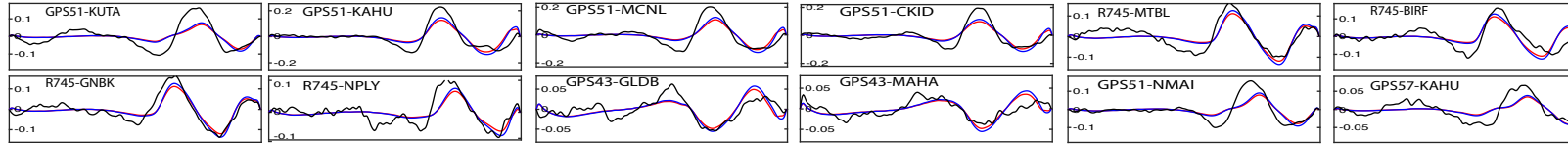
Map of ionospheric pierce point positions for sTEC stn-sat pairs



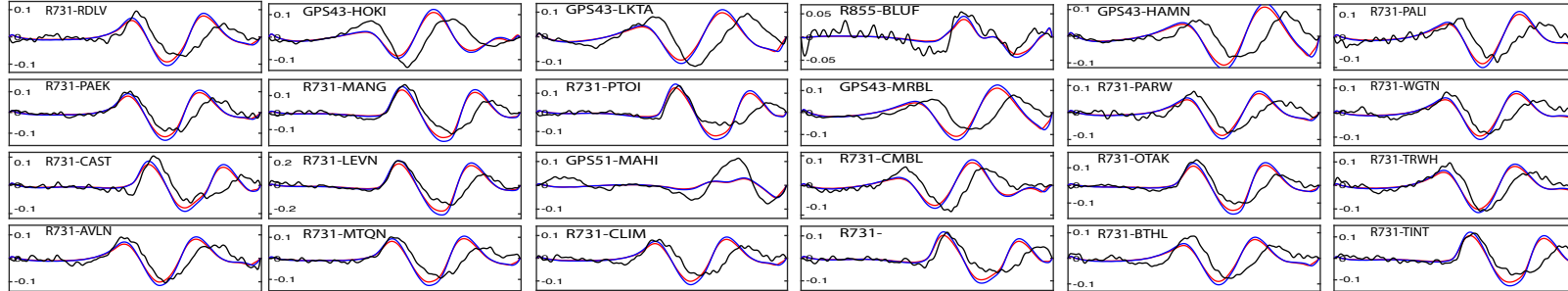
Signals west to the epicenter



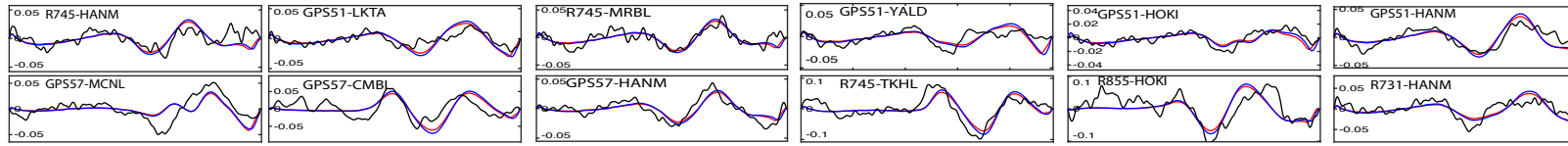
Signals over Northern Island



Signals over the Ocean



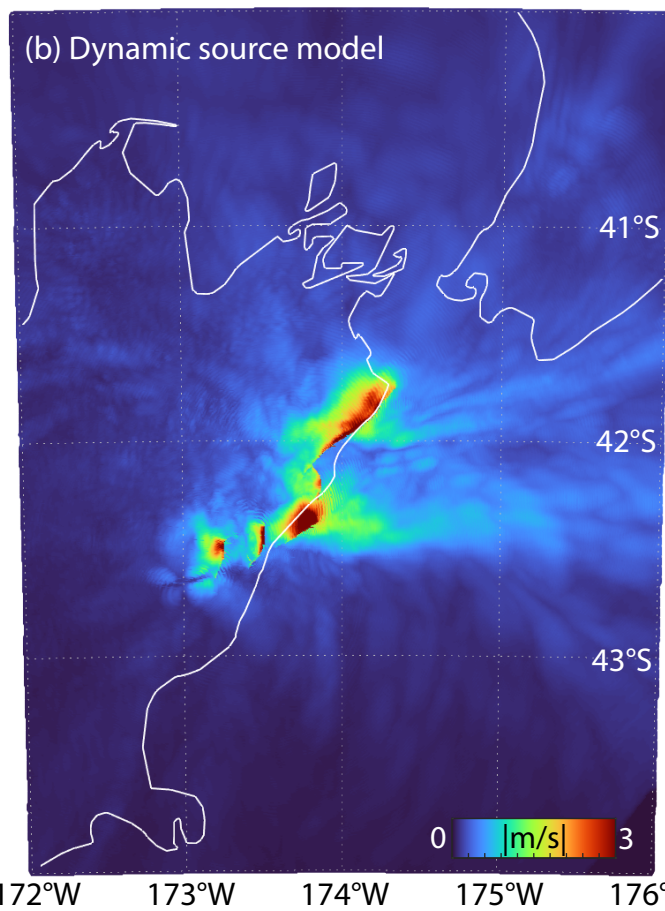
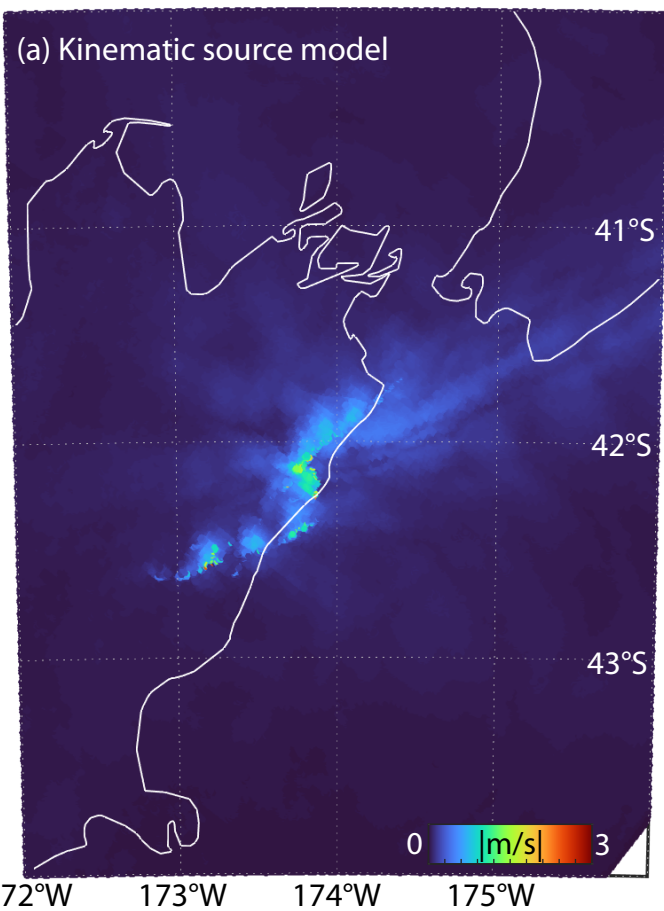
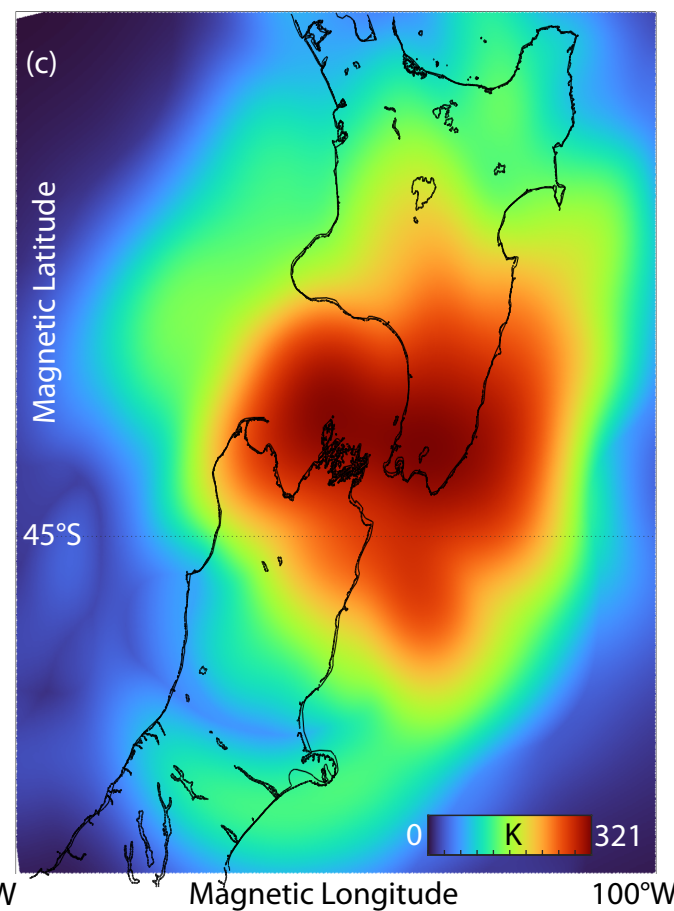
Small amplitude signals



204 sec 600 1000 204 sec 600 1000 204 sec 600 1000 204 sec 600 1000 204 sec 600 1000 204 sec 600 1000

Figure 4.

Maximum reached absolute vertical velocities at the surface

Max absolute T' at 300 km

(d) Comparison of observed (blue) and synthetic sTEC signals from Sim #1 (red) and Sim #3 (yellow)

